

# Water vapour profiles by ground-based FTIR Spectroscopy: study for an optimised retrieval and its validation

by M. Schneider, F. Hase, and T. Blumenstock

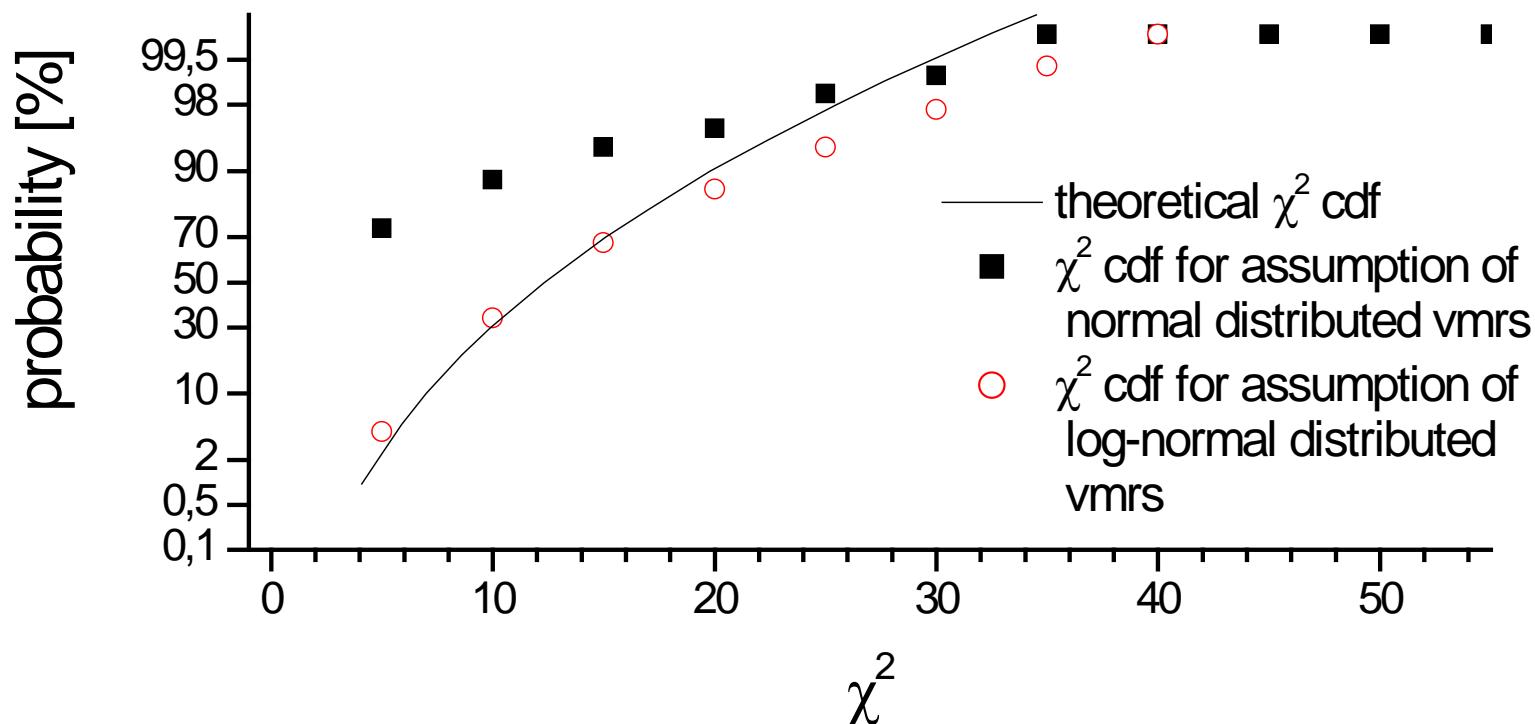
1. Inversion on a logarithmic scale, why ?
2. Error characterization (... towards an optimal strategy for UT H<sub>2</sub>O retrieval)
3. 7-year record of water vapour above Izaña observatory
4. Summary and outlook

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6, 811-830, 2006

1. Inversion on a logarithmic scale, why ?

Examination of a-priori distribution.  $\chi^2$  test checks for a normal distribution:

$$\chi^2 = (x - x_a)^T S_a^{-1} (x - x_a)$$



## 1. Inversion on a logarithmic scale, why ?

The cost function

$$\sigma^{-2}(y - Kx)^T(y - Kx) + (x - x_a)^T S_a^{-1}(x - x_a)$$

is only correctly posted if state vector is transformed on a logarithmic scale !

On a linear scale a wrong a-priori distribution is assumed !

Then the term

$$(x - x_a)^T S_a^{-1}(x - x_a)$$

provides for an overestimation of small  $x$  and an underestimation of large  $x$  !

Error estimation is performed by a „Monte Carlo“ method. Analytic error estimation like proposed by Rodgers (1990) is not appropriate due to non-linearities.

1. Forward calculation of assumed H<sub>2</sub>O profile
2. Introducing of errors (measurement noise, temperature profile, ILS, spectroscopic parameter, ...)
3. Inversion of the simulated spectra

This „Monte Carlo“ error estimation works only if we apply a large ensemble of H<sub>2</sub>O profiles, which obey the real H<sub>2</sub>O statistics ! We apply 500 ptu-sonde measurements of the years 1999 and 2000.

Errors are commonly presented as a mean (systematic error) and variance (random error).

Here we present them in a more general manner: by least squares fits

→ difference of regression curve from diagonal: offset + slope of regression line (mean + sensitivity as systematic error)

→ scattering around the regression curve (residual variance as random error):

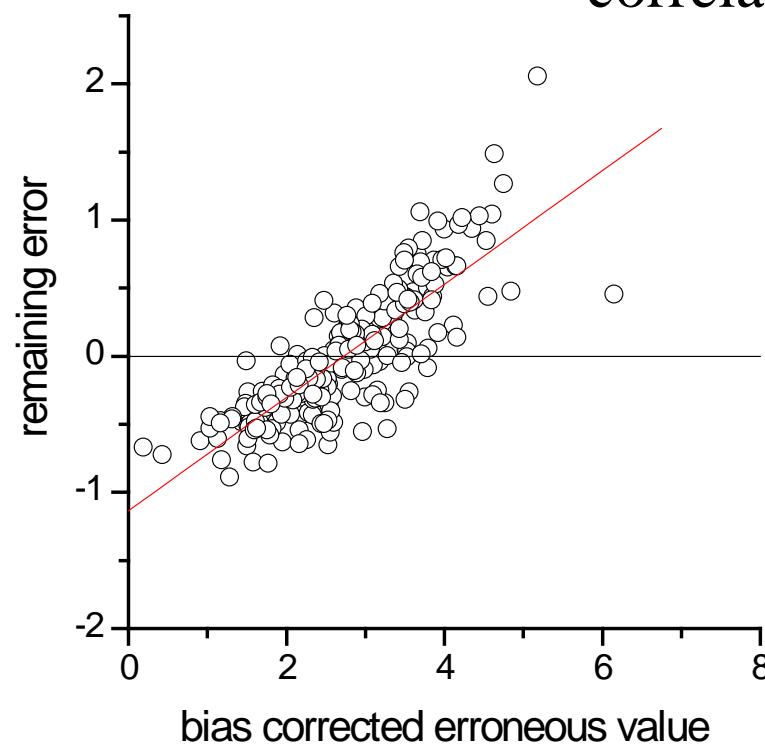
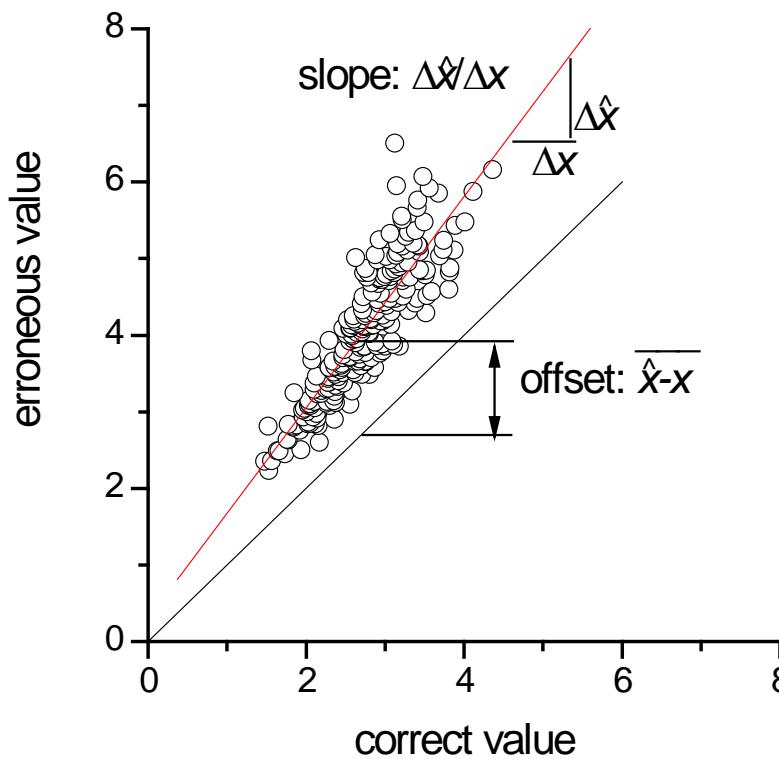
$$\frac{\sigma_{\varepsilon\_reg}}{\sigma_{\hat{x}}} = \sqrt{1 - \rho^2}$$

## Error estimation by means of linear least squares fit

Why? — there are two kind of systematic errors:

1. mean error (bias)

2. sensitivity error  
(slope $\neq 1$  or no linear correlation)



In the following the errors of lower, middle, and upper tropospheric H<sub>2</sub>O are

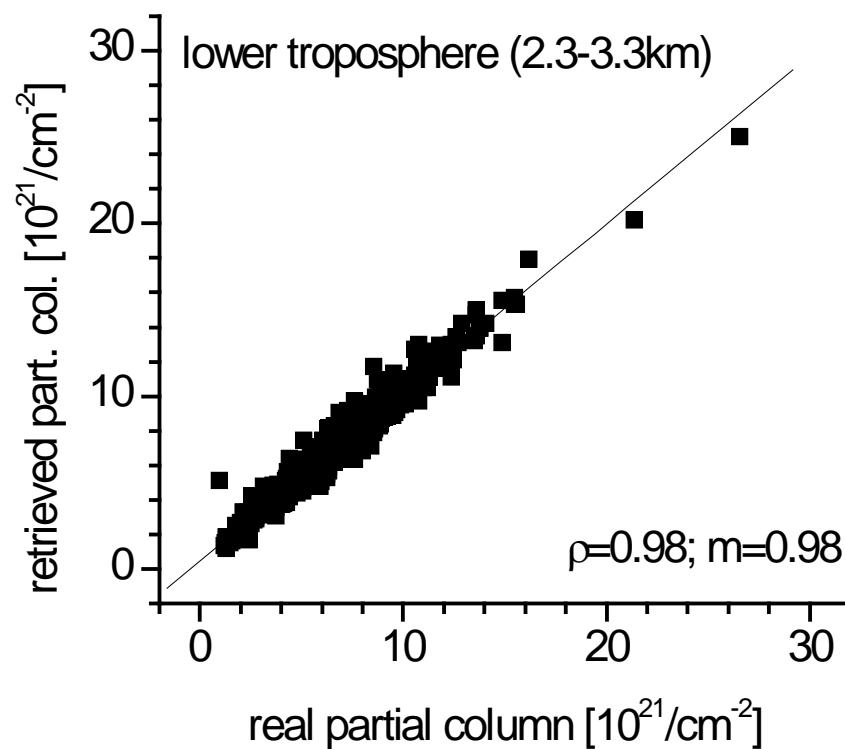
1. estimated by Monte Carlo simulations

and

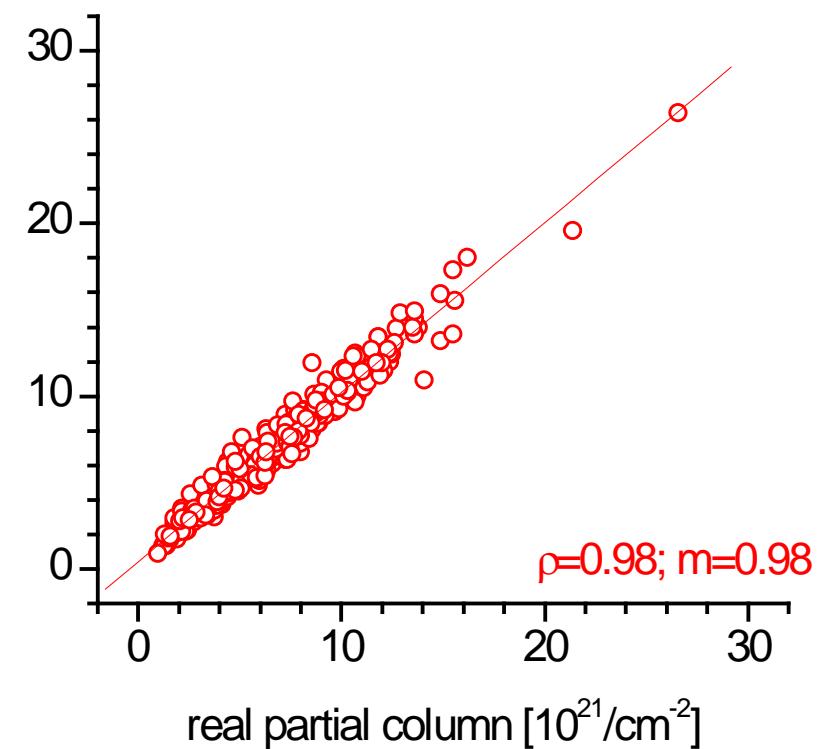
2. validated by comparing H<sub>2</sub>O from FTIR measurements with daily ptu-sondes

## Estimation of total FTIR error (2.3-3.3km):

linear scale

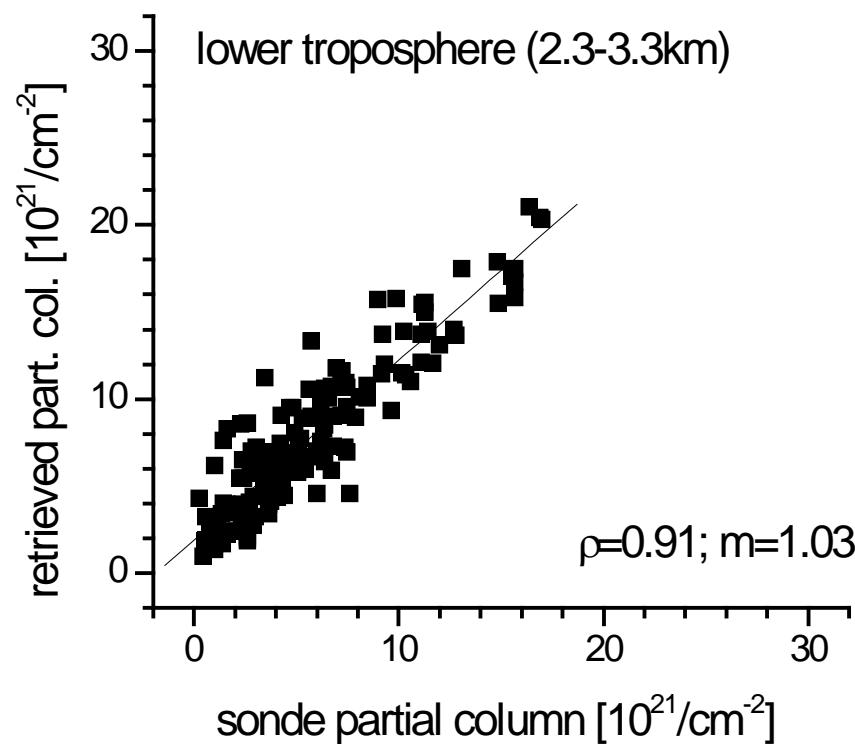


logarithmic scale

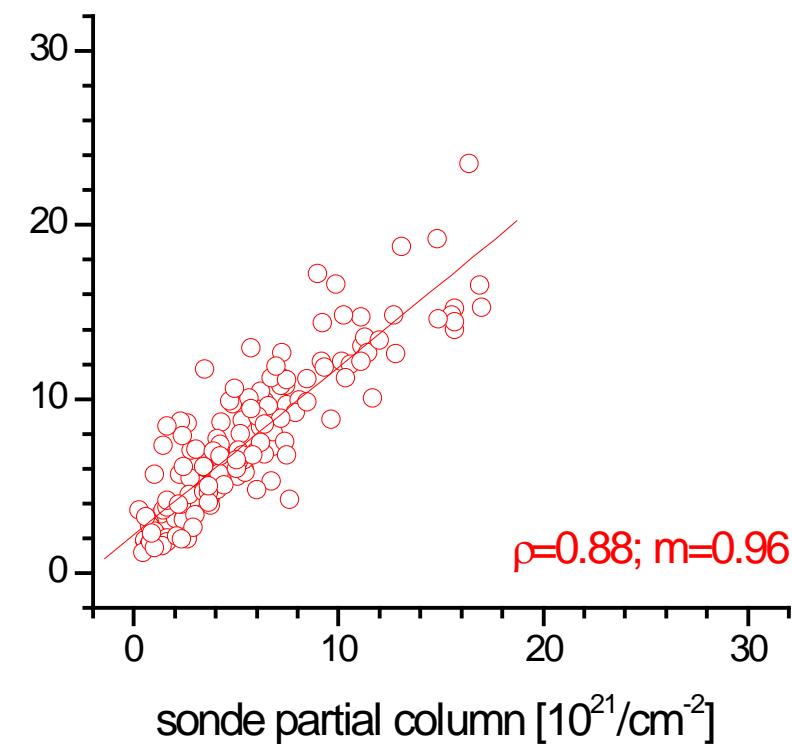


**FTIR vs. ptu-sondes** at 2.3-3.3km. Problem: detection of different regions (FTIR: boundary layer; sonde: free troposphere)

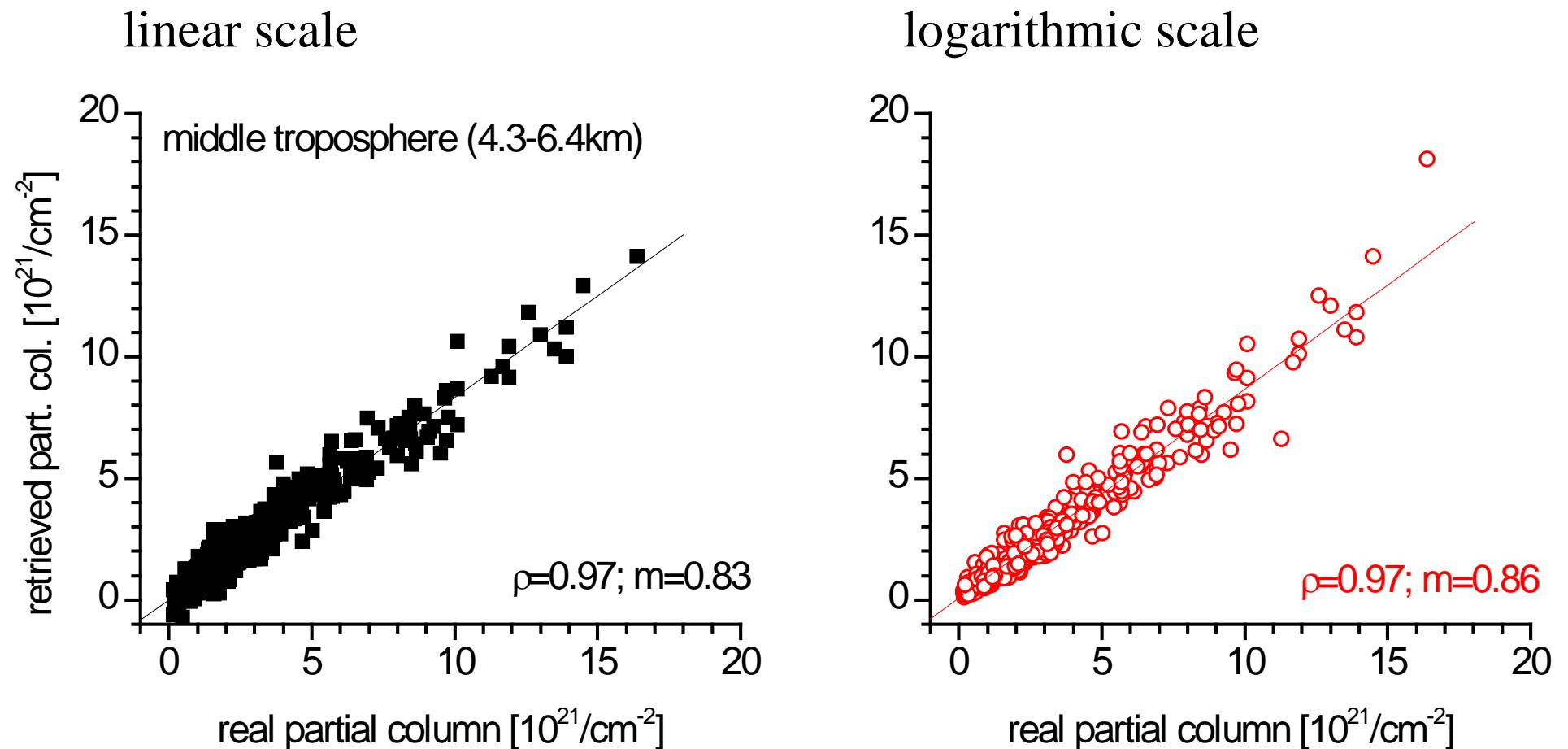
linear scale



logarithmic scale

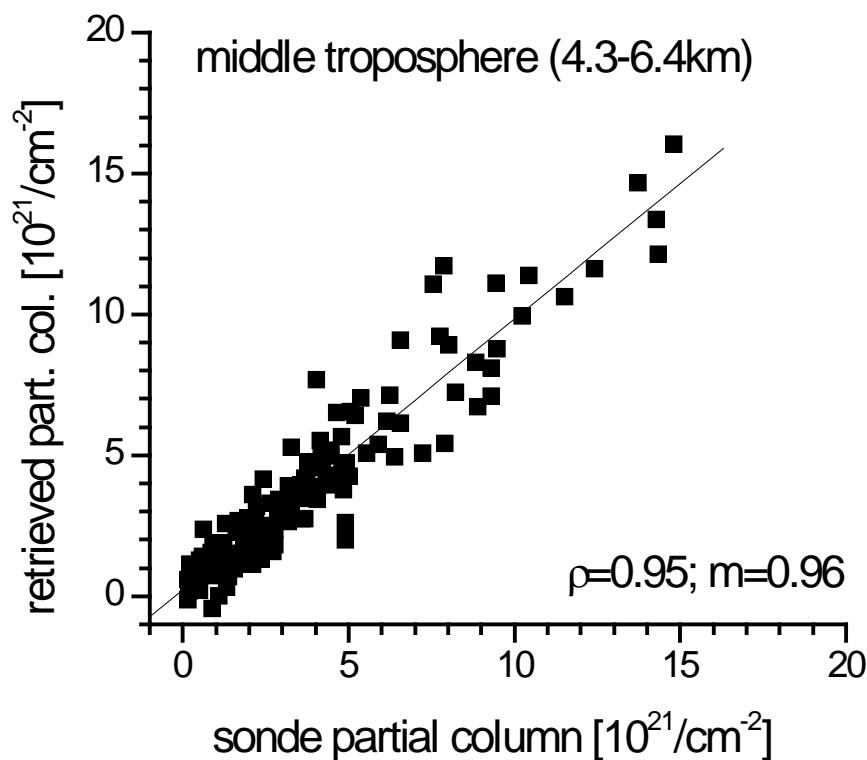


## Estimation of total FTIR error (4.3-6.4km):

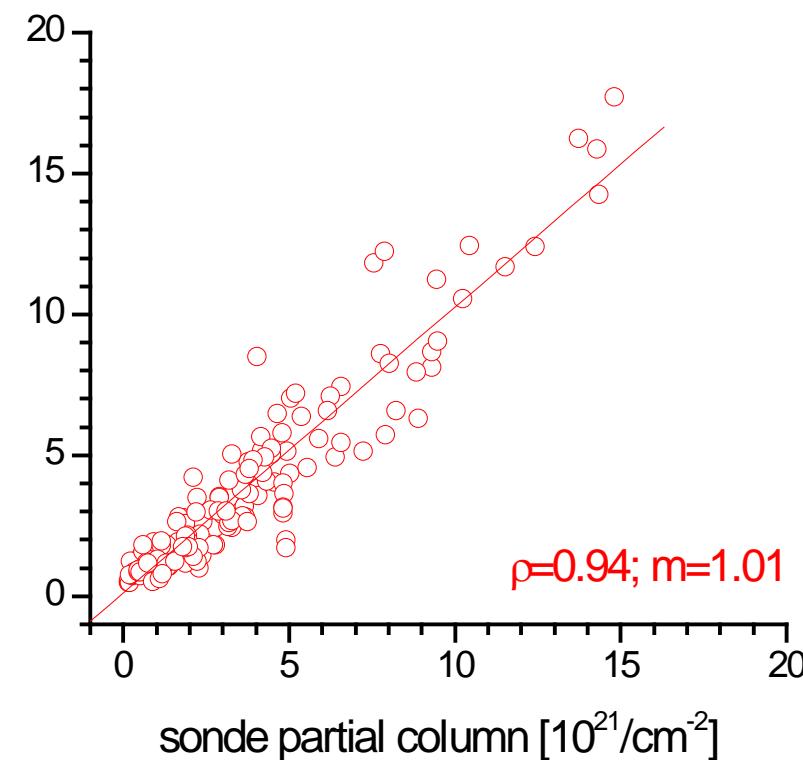


**FTIR vs. ptu-sonde** at 4.3-6.4km:

linear scale

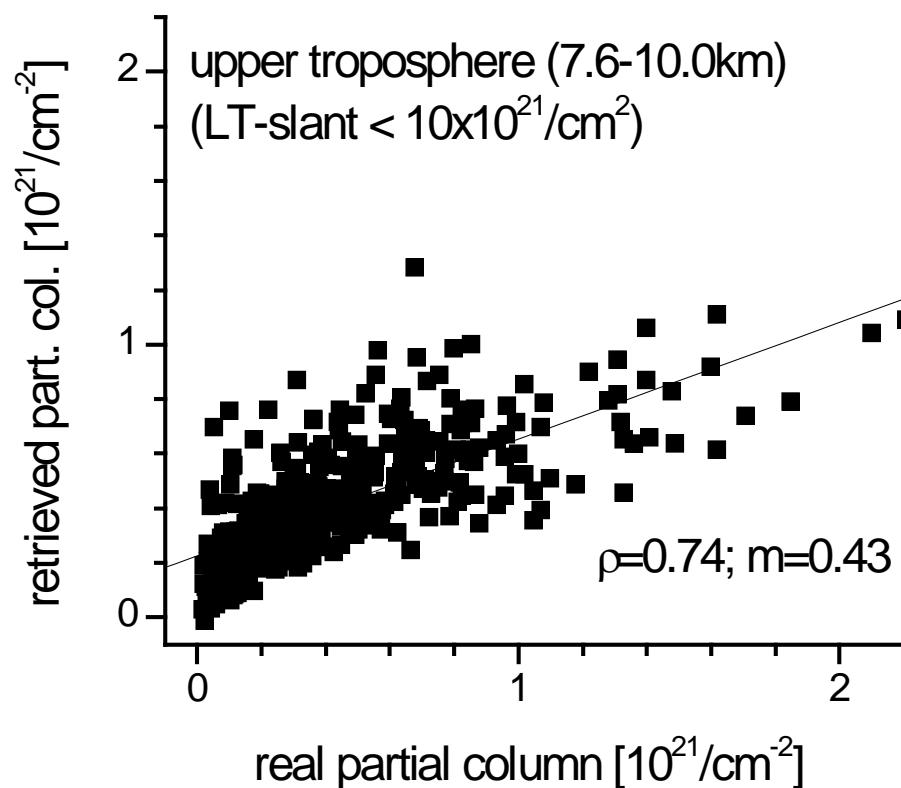


logarithmic scale

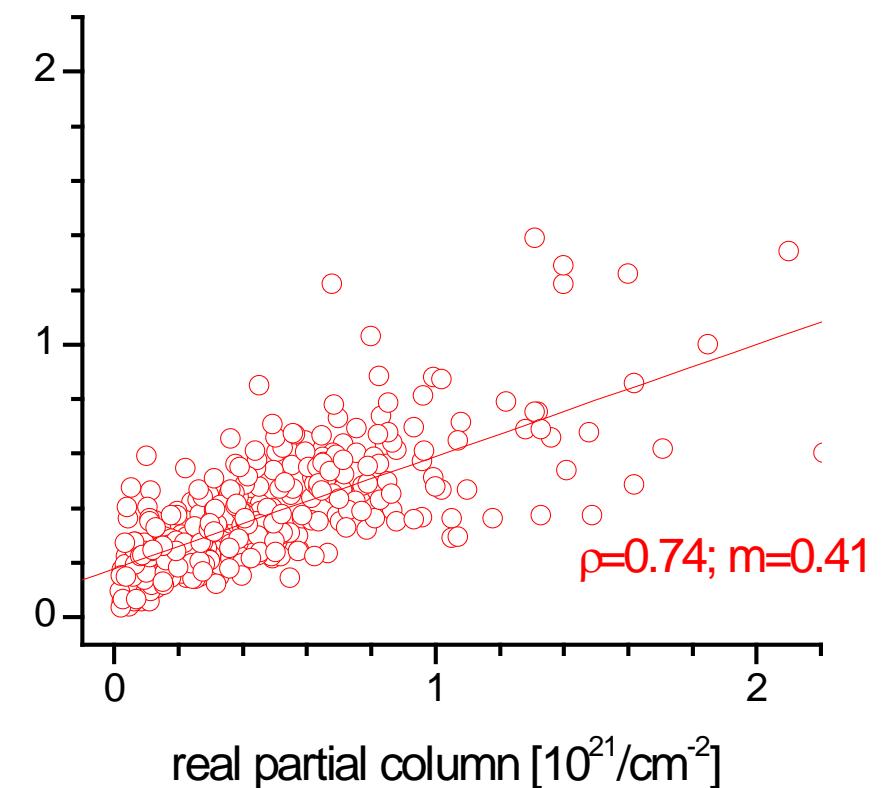


## Estimation of total FTIR error (7.6-10.0km):

linear scale

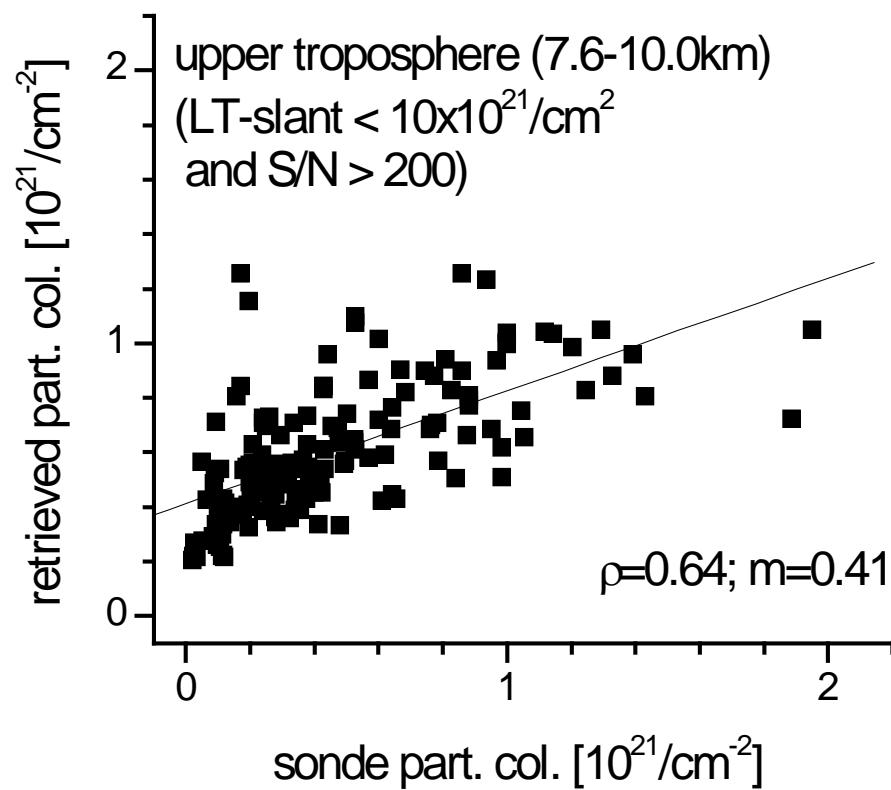


logarithmic scale

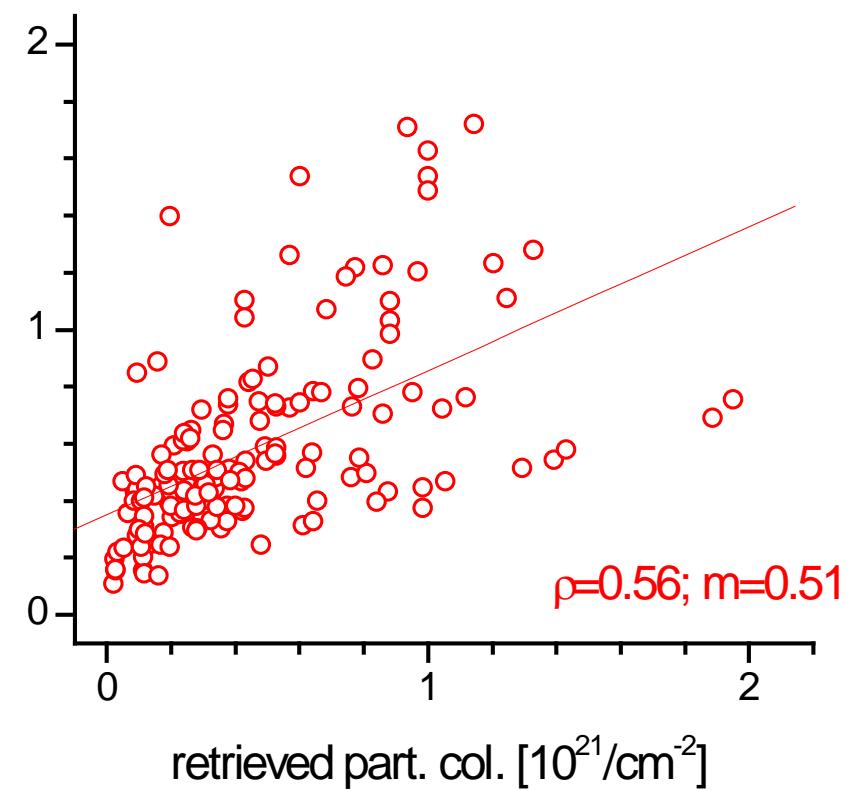


**FTIR vs. ptu-sonde** at 7.6-10.0km:

linear scale

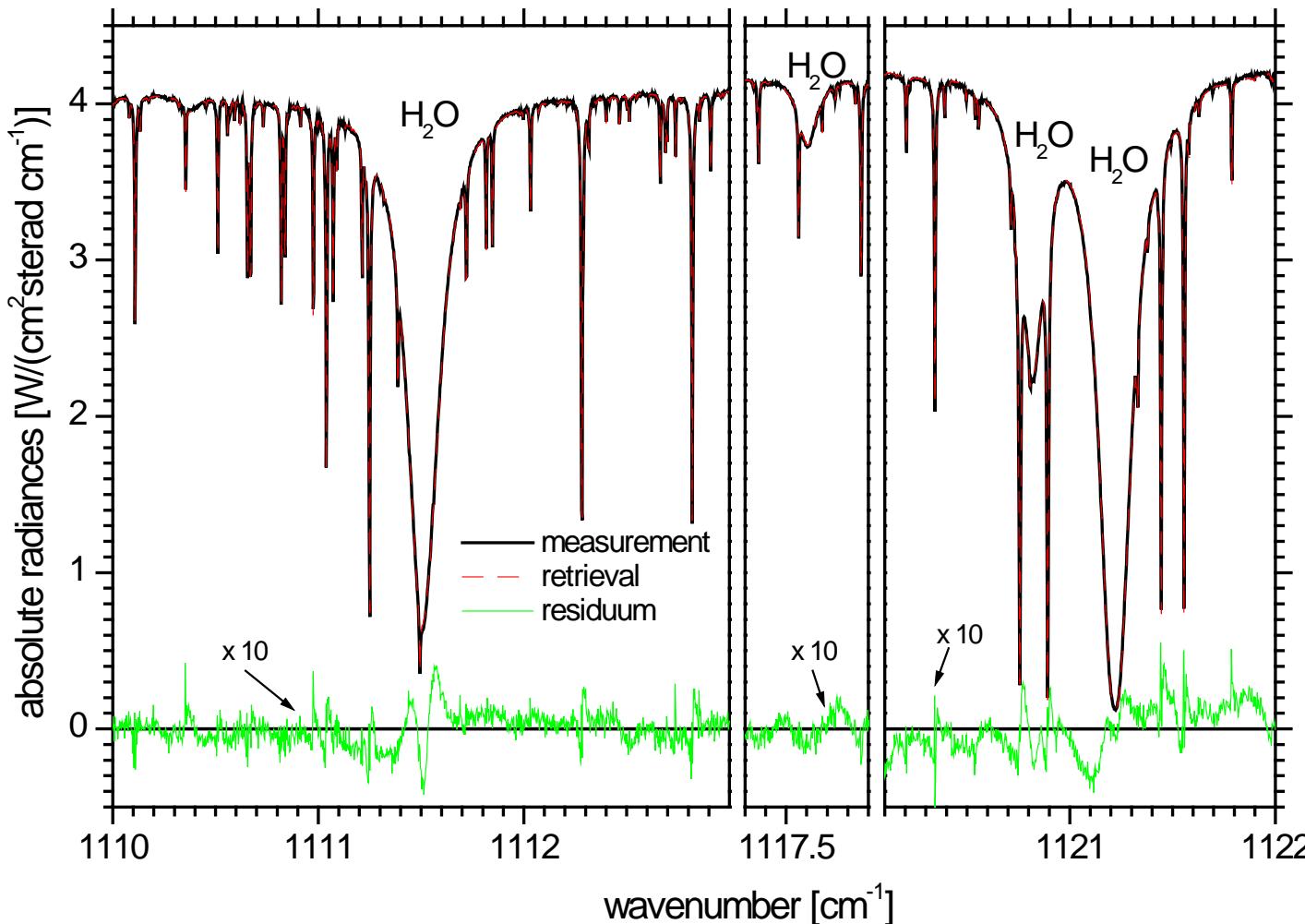


logarithmic scale



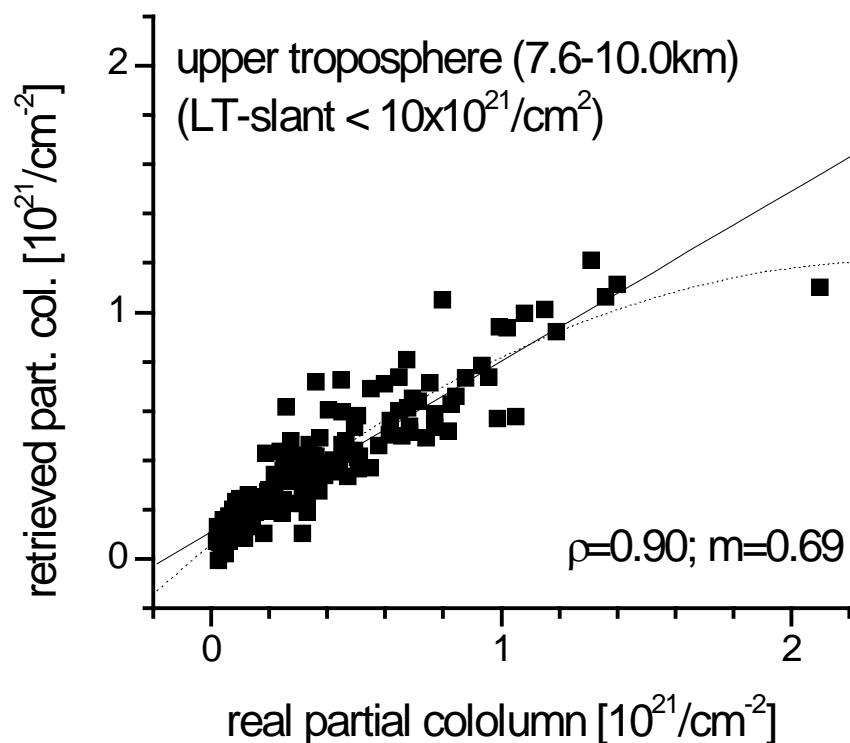
Can we reduce the error of the retrieved UT  $\text{H}_2\text{O}$  amount ?

Case A: Yes, when absorption lines are unsaturated !

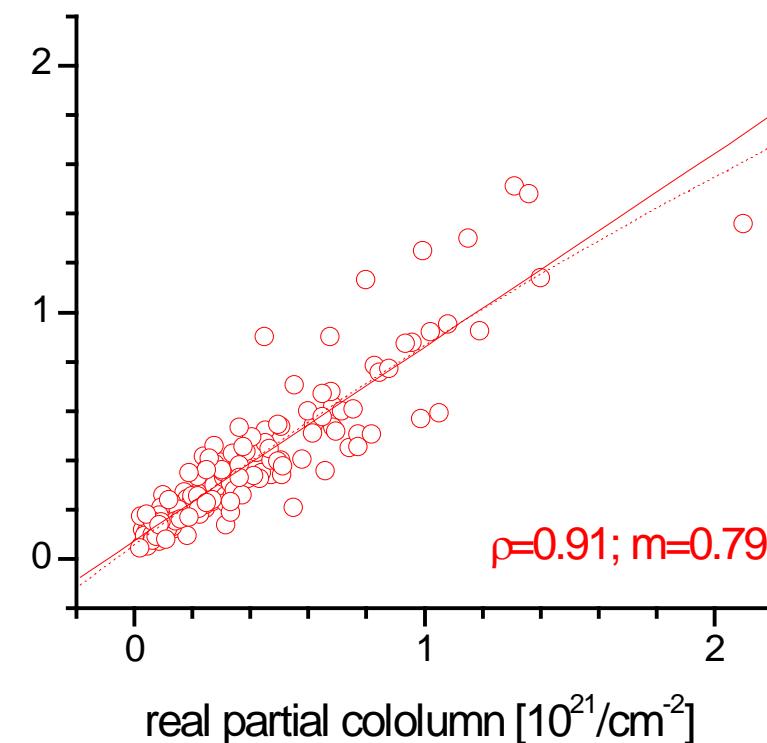


Upper troposphere (Case A): **Estimation** of total FTIR error for LT slant below  $10 \times 10^{21} \text{cm}^{-2}$  (7.6-10.0km):

linear scale

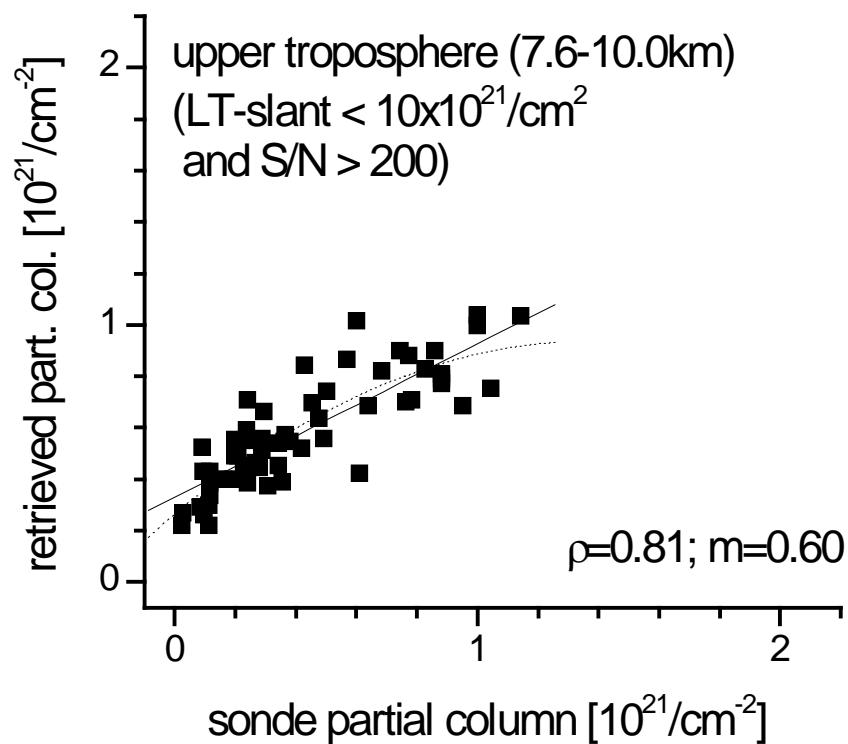


logarithmic scale

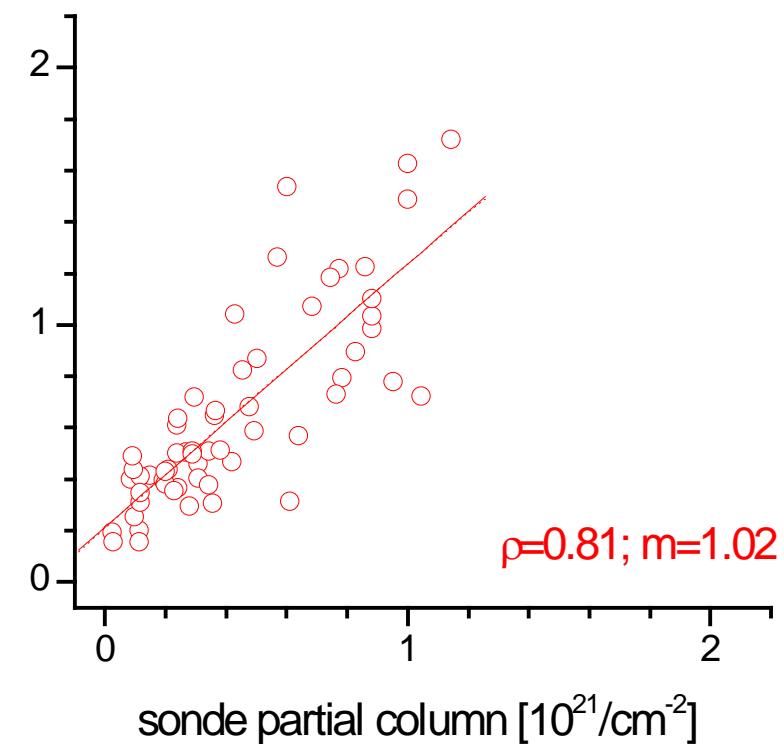


Upper troposphere (Case A): FTIR vs. ptu-sonde at 7.6-10.0km for LT slant below  $10 \times 10^{21} \text{cm}^{-1}$ :

linear scale

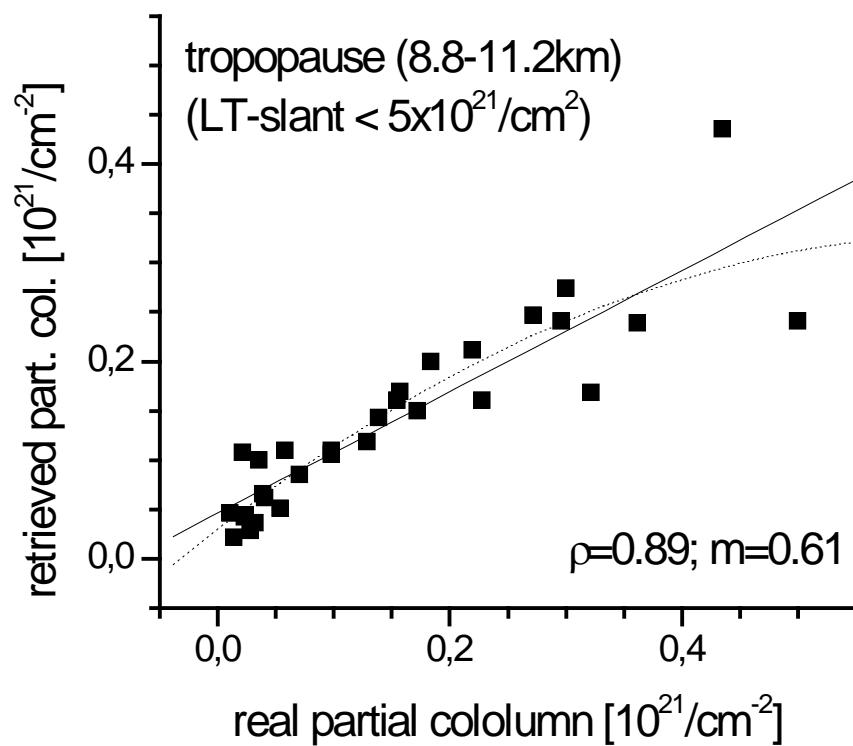


logarithmic scale

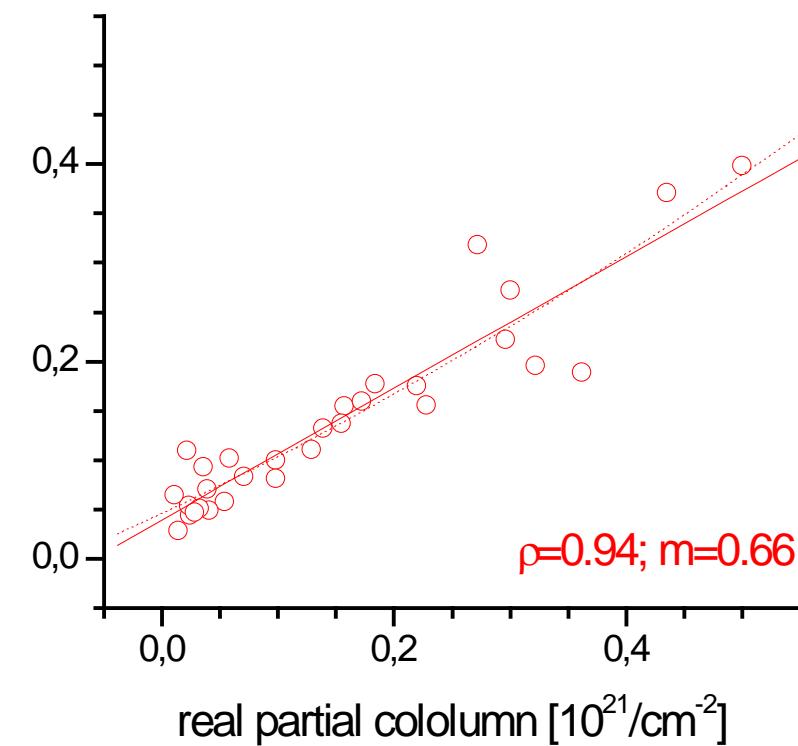


Upper troposphere (Case A): Estimation of total FTIR error for LT slant  
below  $5 \times 10^{21} \text{cm}^{-2}$  (8.8-11.2km):

linear scale

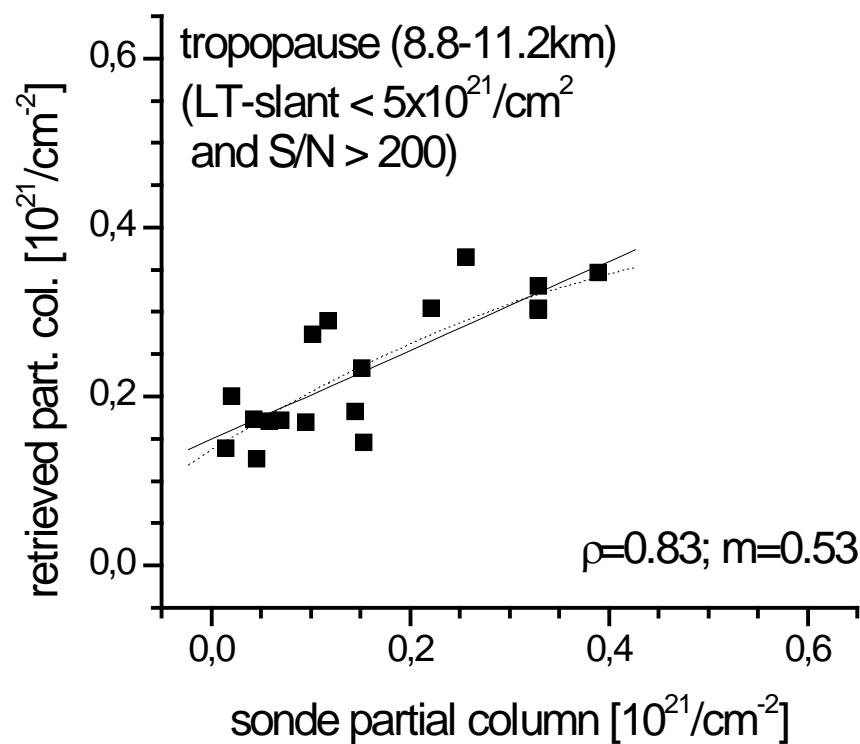


logarithmic scale

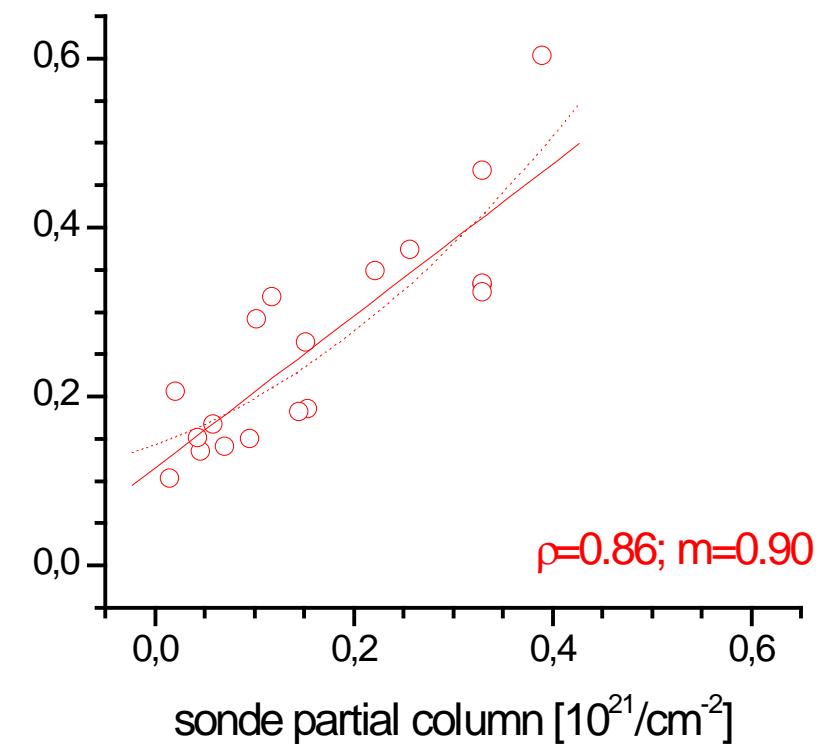


Upper troposphere (Case A): FTIR vs. ptu-sonde at 8.8-11.2km for LT slant below  $5 \times 10^{21} \text{cm}^{-1}$ :

linear scale



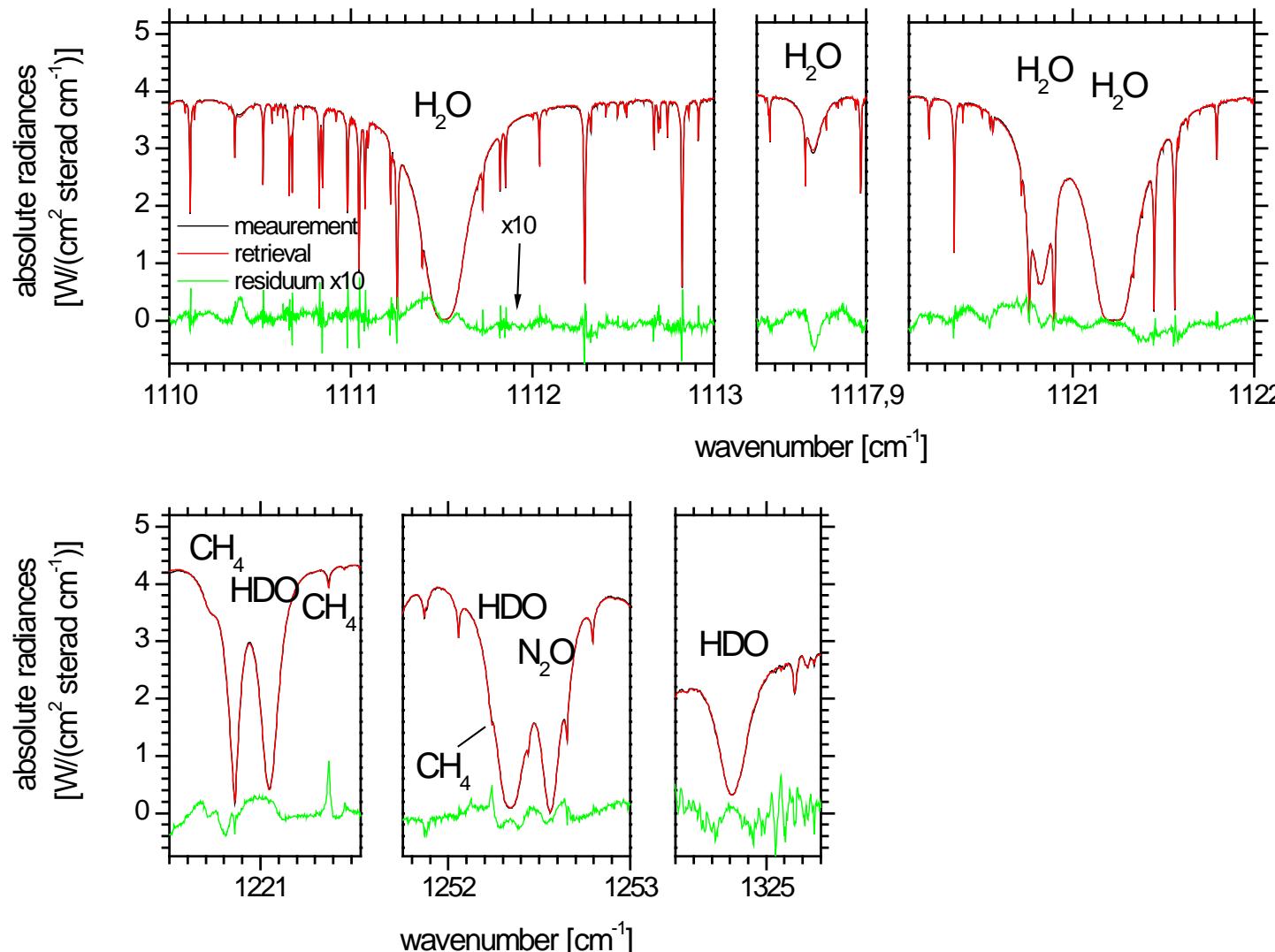
logarithmic scale



2. Error estimations

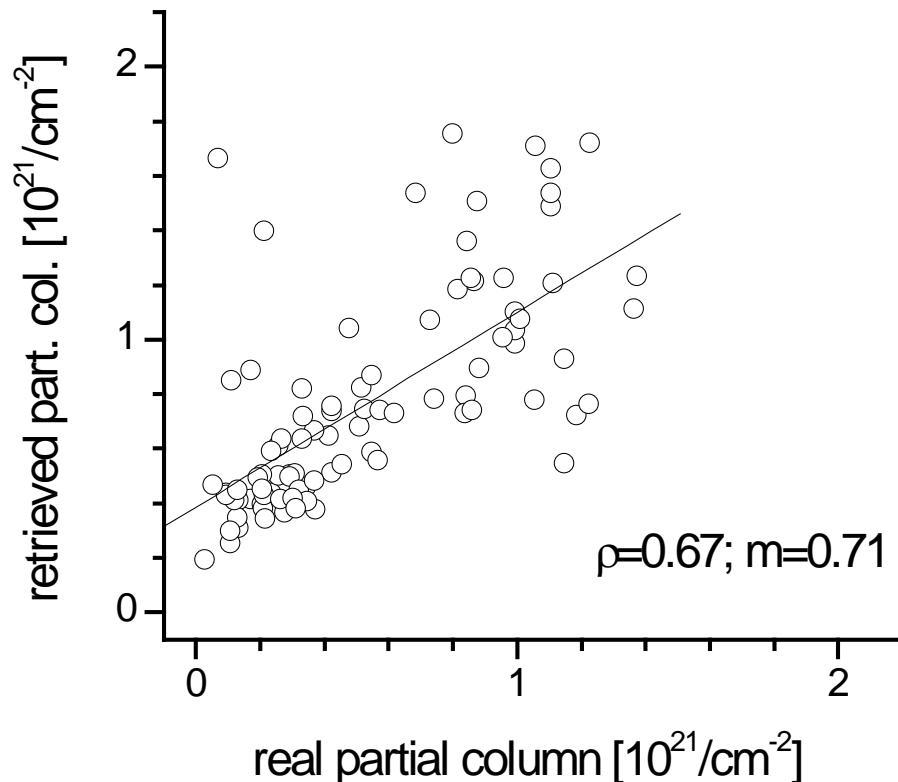
Can we reduce the error of the retrieved UT  $\text{H}_2\text{O}$  amount ?

Case B: Yes, when strong and moderately strong lines are fitted simultaneously !

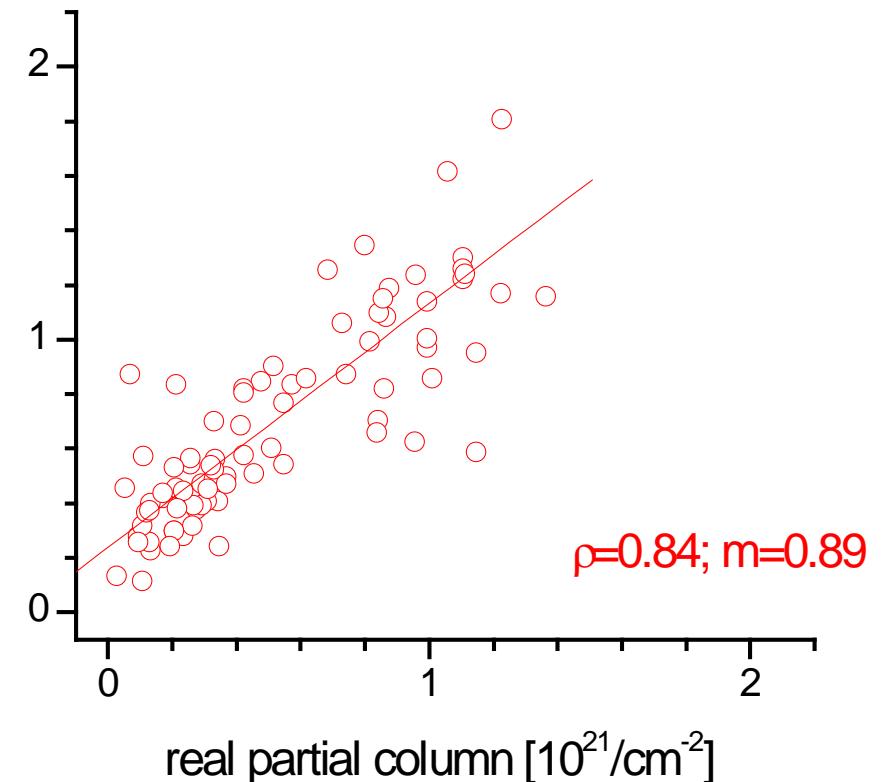


Upper troposphere (Case B): FTIR vs. ptu-sonde at 7.6-10.0km (LT slant below  $25 \times 10^{21} \text{cm}^{-2}$ ):

strong lines

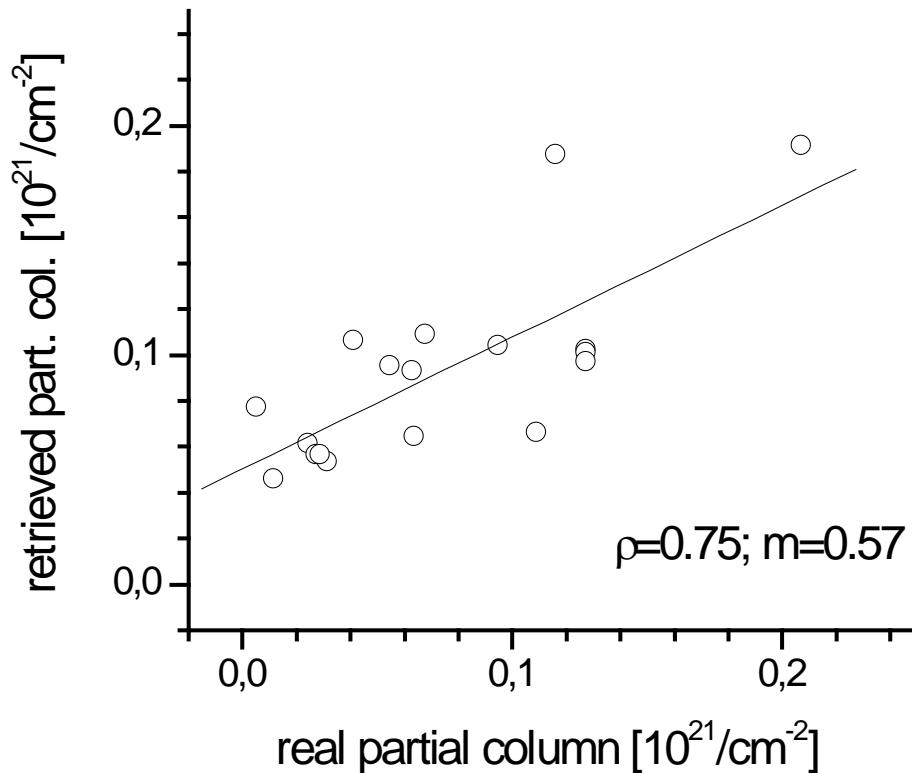


strong and moderately strong lines

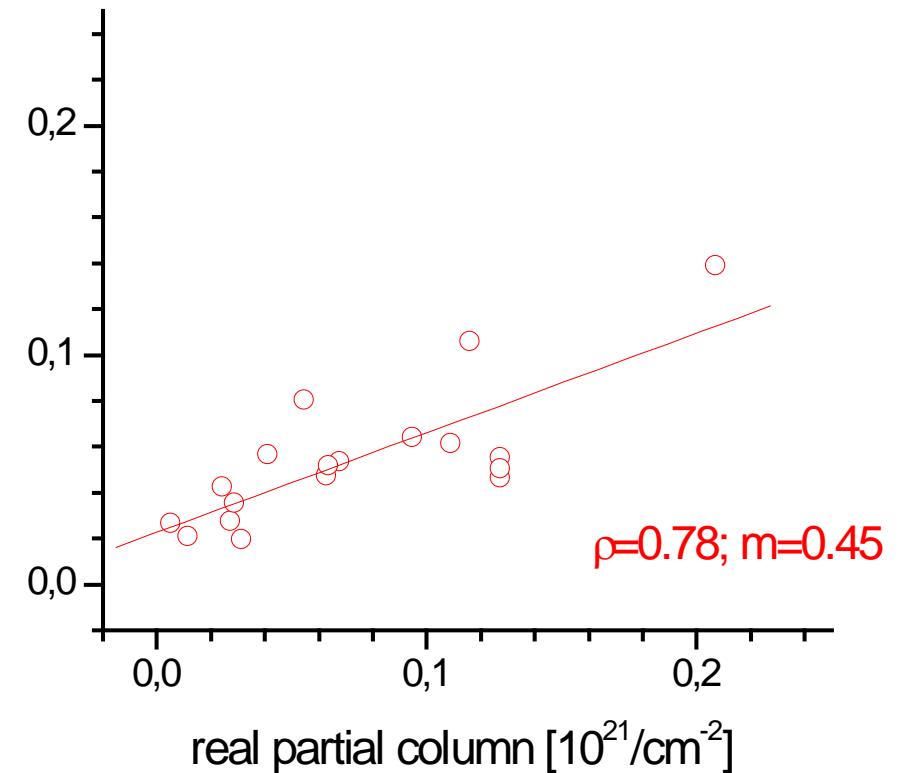


Upper troposphere (Case B): FTIR vs. ptu-sonde at 10.0-12.4km (LT slant below  $5 \times 10^{21} \text{cm}^{-2}$ ):

strong lines



strong and moderately strong lines



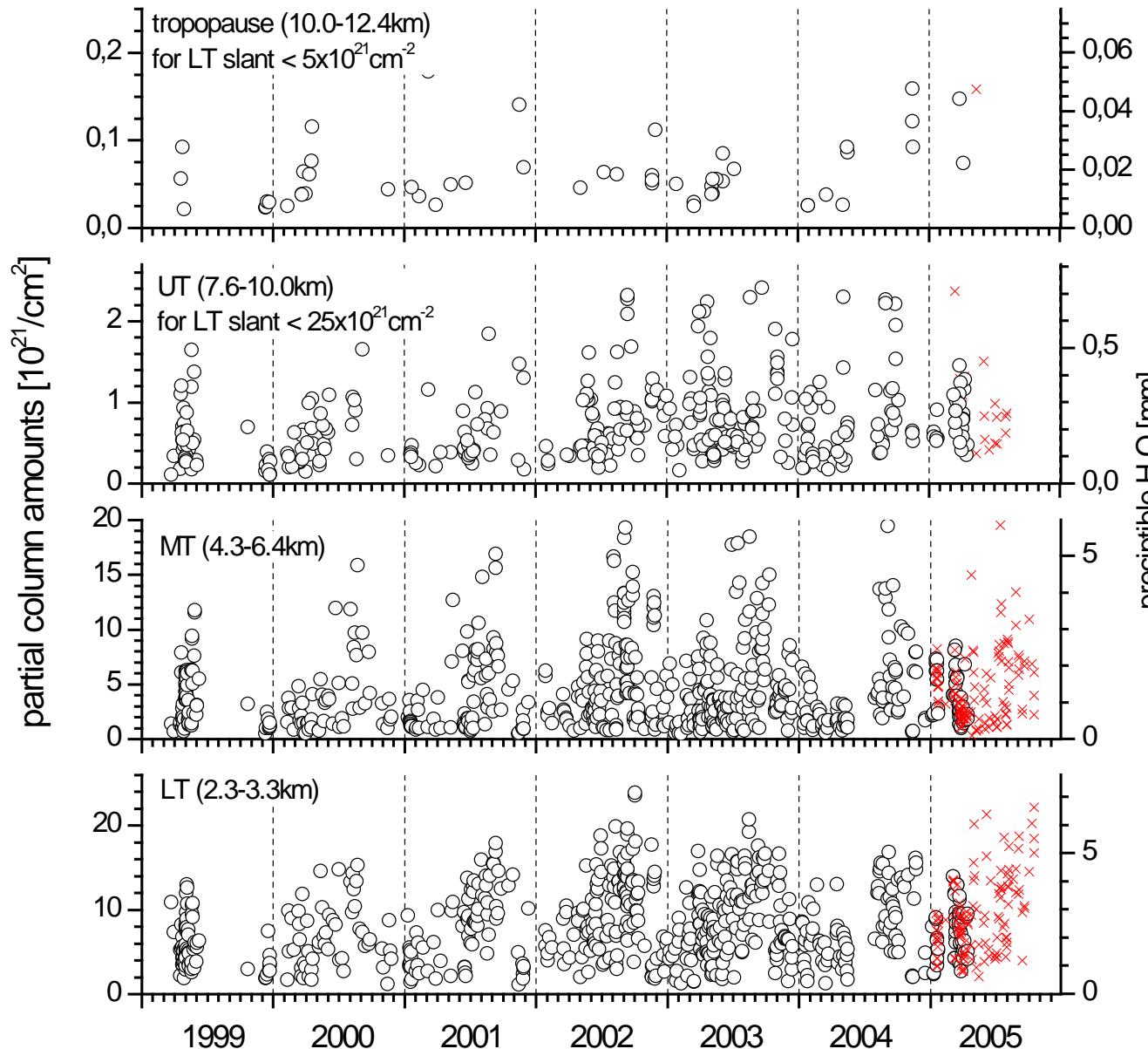
Recipe for retrieval of upper tropospheric H<sub>2</sub>O:

- Only retrieval on a logarithmic scale provides for a correctly posted cost function → this reduces the systematic errors if compared to a retrieval on linear scale. It leads to consistent time series and a good sensitivity for UT H<sub>2</sub>O amounts
- Simultaneous fit of strong and moderately strong lines provides for best exploitation of spectra → makes continuous observation of UT H<sub>2</sub>O feasible
- Most important errors are: smoothing error, ILS, line parameter, and temperature profile

# Forschungszentrum Karlsruhe

## in der Helmholtz-Gemeinschaft

### 3. 7-year record of water vapour above Izaña observatory



Above 9km retrieval requires unsaturated  $\text{H}_2\text{O}$  lines → LT slant below  $5 \times 10^{21} \text{ cm}^{-2}$  (in Izaña only for 10% of all measurements)

Above 7.5km retrieval requires moderate LT  $\text{H}_2\text{O}$  amounts and simultaneous fit of strong and moderately strong lines

Up to 7km retrieval possible under all measurement conditions

Our study shows the following:

1. FTIR well-suited for continuous monitoring of lower and middle tropospheric H<sub>2</sub>O amounts.
2. For upper tropospheric H<sub>2</sub>O amounts a continuous monitoring is tricky, but feasible by FTIR, if:
  - A: the inversion is perform on a log-scale
  - B: strong and moderately strong lines are fitted simultaneously

Future work:

1. Produce continuous time series of UT water vapour from many historic FTIR measurements (e.g. measurements at Jungfraujoch or Kitt Peak could produce unique continuous 20-year records !)
2. Further improvements are still possible for dryer or higher situated sites: we could apply stronger H<sub>2</sub>O lines → improved sensitivity at higher altitudes. Detection of lower stratospheric water vapour variability from Jungfraujoch ?
3. Retrieval of HDO/H<sub>2</sub>O

Thank You !!!!!!!

Summary of differences between FTIR and ptu sonde data (sum of errors of sonde and FTIR). Theoretical estimations of FTIR errors are in brackets:

linear scale:

	total	2.3-3.3km	4.3-6.4km	7.6-10.0km	8.8-11.2km
random	<b>25 (4)</b>	<b>40 (21)</b>	<b>32 (24)</b>	<b>54 (50)</b>	<b>56 (47)</b>
systematic <sup>(A)</sup>	<b>+6 (0)</b>	<b>+3 (-3)</b>	<b>-4 (-6)</b>	<b>-40 (-31)</b>	<b>-47 (-38)</b>

logarithmic scale:

	total	2.3-3.3km	4.3-6.4km	7.6-10.0km	8.8-11.2km
random	<b>25 (4)</b>	<b>47 (22)</b>	<b>33 (24)</b>	<b>58 (49)</b>	<b>51 (42)</b>
systematic <sup>(A)</sup>	<b>+6 (-1)</b>	<b>-4 (-4)</b>	<b>+1 (-1)</b>	<b>+2 (-23)</b>	<b>-10 (-33)</b>

(A): systematic spectroscopic line parameter errors are not considered

Upper troposphere (Case B): **Estimation** of total FTIR error at 7.6-  
10.0km (LT slant below  $25 \times 10^{21} \text{cm}^{-2}$ ):

strong lines

strong and moderately strong lines

Upper troposphere (Case B): **Estimation** of total FTIR error at 7.6-10.0km  
(LT slant below  $25 \times 10^{21} \text{cm}^{-1}$ ):

strong lines

strong and moderately strong lines

What about the averaging kernels ?

3. Vertical resolution

In the case of water vapour the averaging kernels only contain limited information about the sensitivity of the measurements.

Reason:

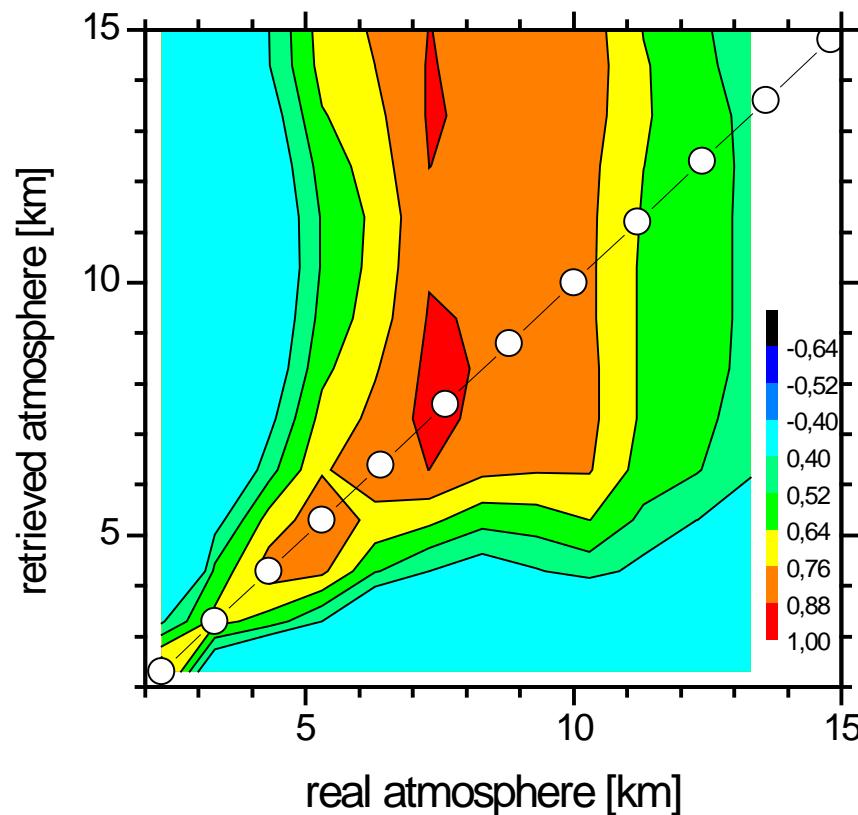
1. Non-linearities (kernels depend strongly on actual H<sub>2</sub>O profile)
2. variability of H<sub>2</sub>O decreases with height by 4 orders of magnitude  
→ comparison of kernels for different heights is not straight forward !

Alternative representation of sensitivity:

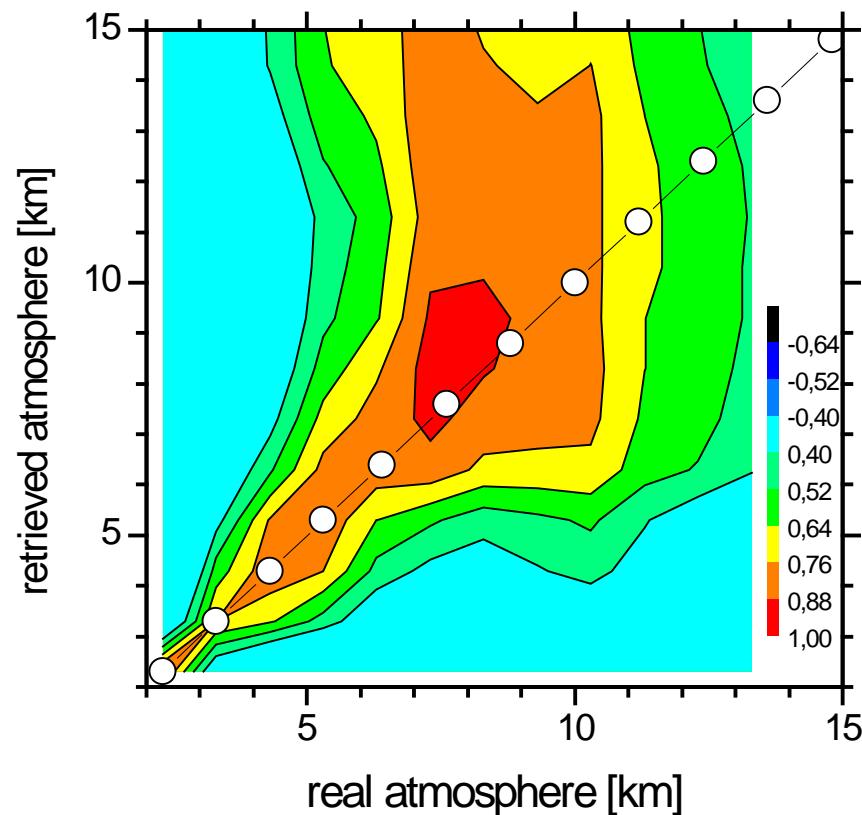
Correlation matrices (correlation between original profiles and inverted profiles). The matrices give a realistic overview of the detectable atmospheric regions. Furthermore, they allow us to perform this sensitivity analysis for a realistic error scenario.

**Estimation** for LT slant column below  $10 \times 10^{21} \text{cm}^{-2}$ :

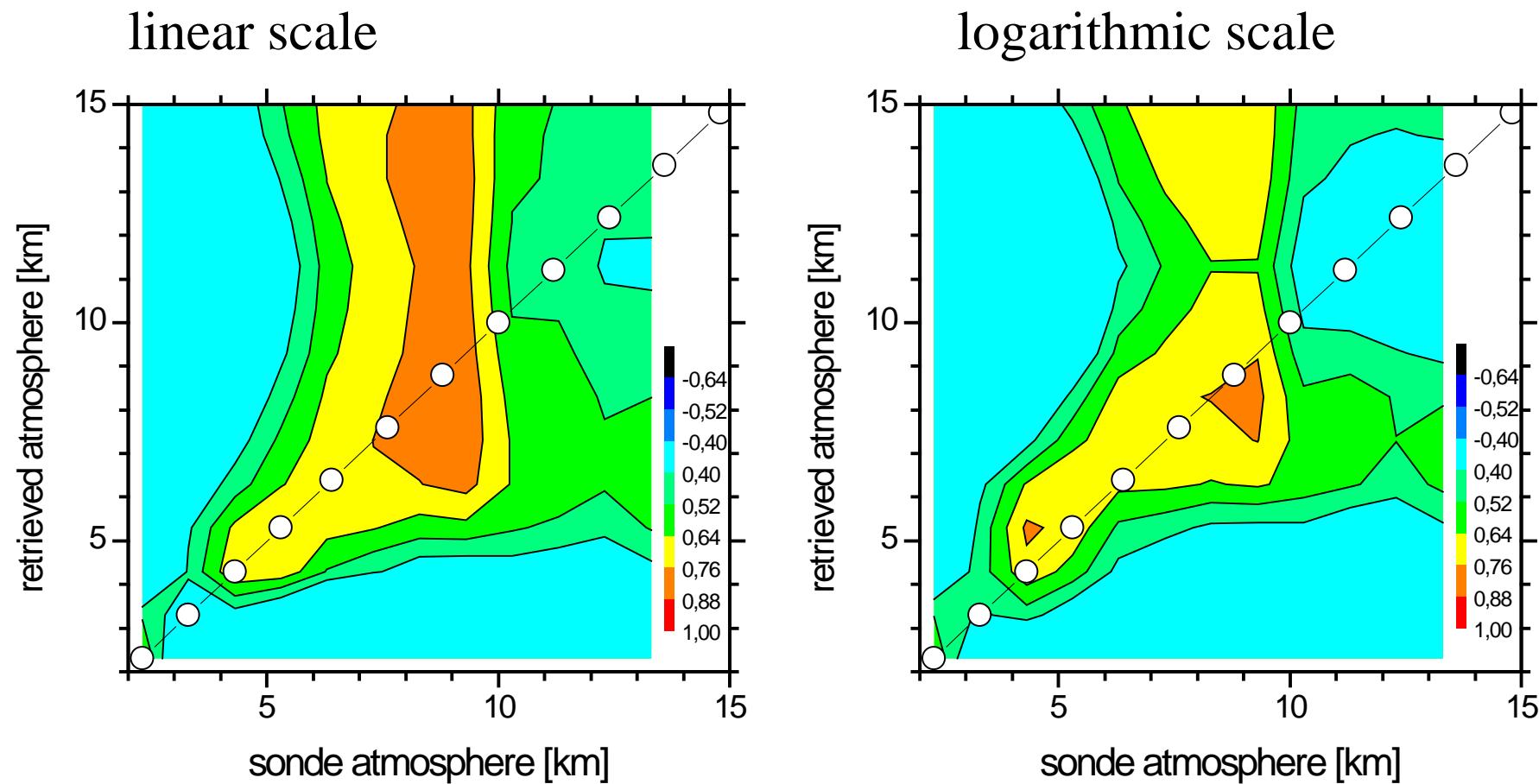
linear scale



logarithmic scale

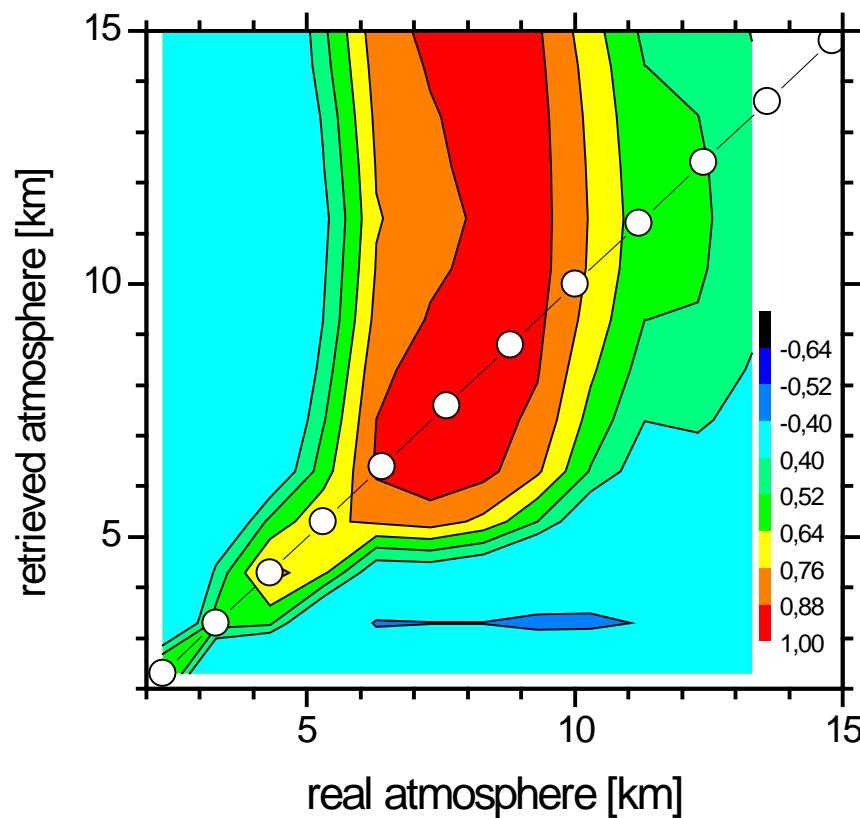


**FTIR vs. sonde** for LT slant below  $10 \times 10^{21} \text{cm}^{-2}$ :

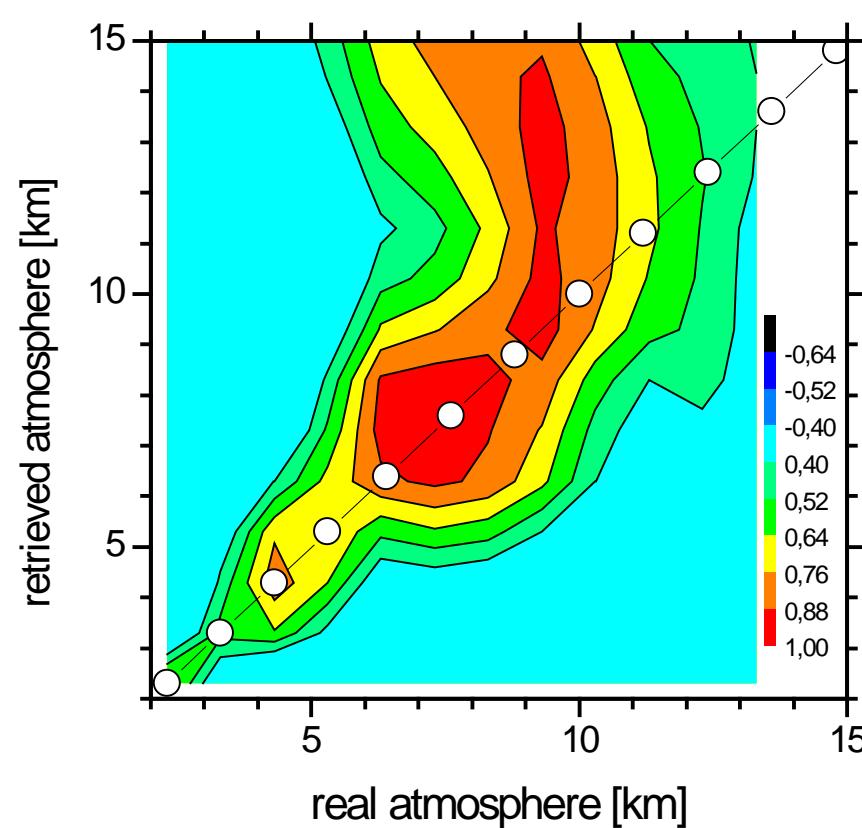


**Estimation** for LT slant column below  $5 \times 10^{21} \text{ cm}^{-2}$ :

linear scale

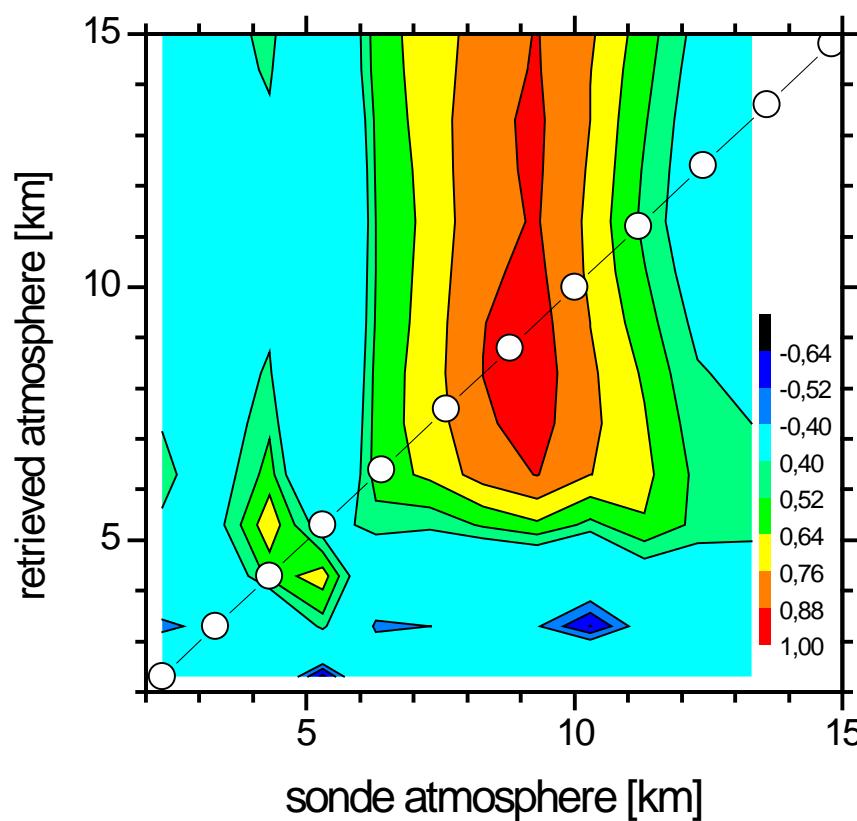


logarithmic scale

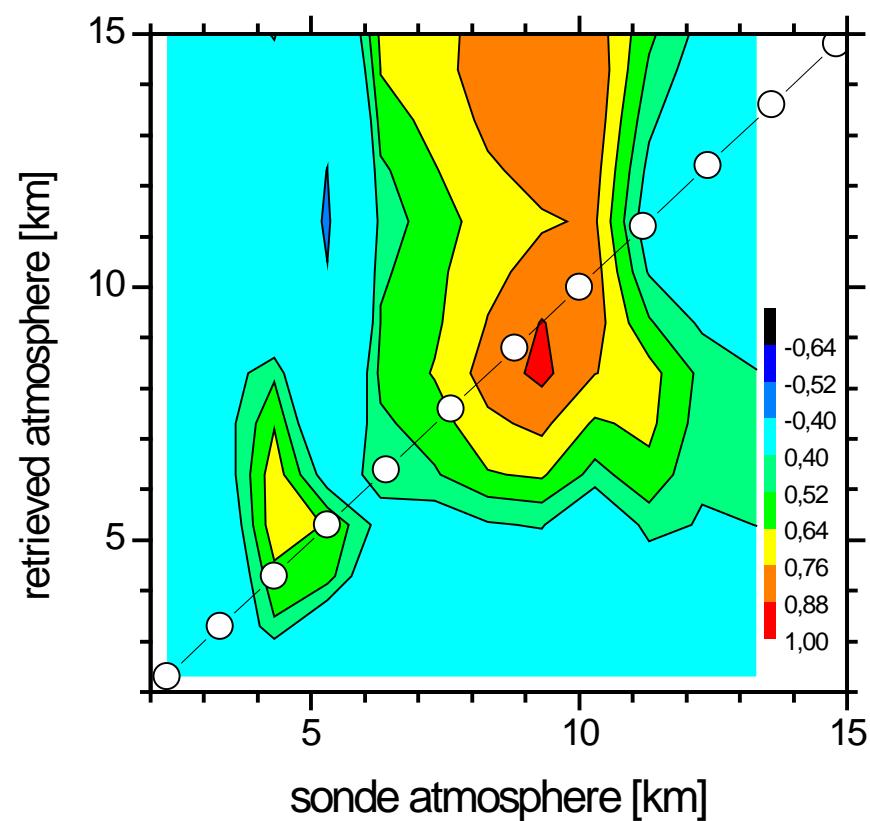


**FTIR vs. sonde** profiles for LT slant  $< 5 \times 10^{21} \text{cm}^{-2}$ :

linear scale

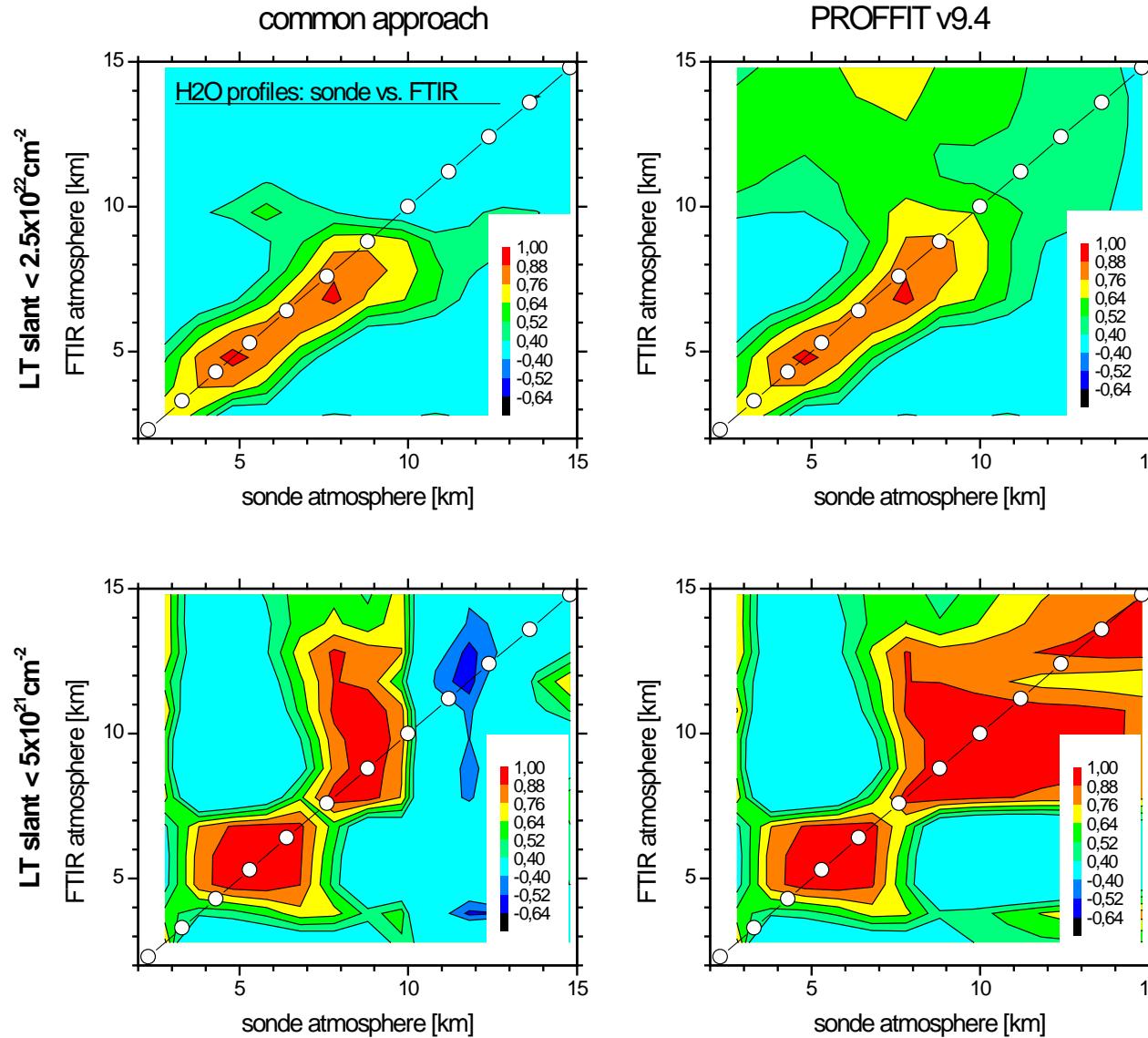


logarithmic scale



Slide from talk “Ground-based remote sensing of tropospheric HDO/H<sub>2</sub>O ratio profiles”

## Empirical validation of H<sub>2</sub>O profiles: ptu-sonde vs. FTIR:



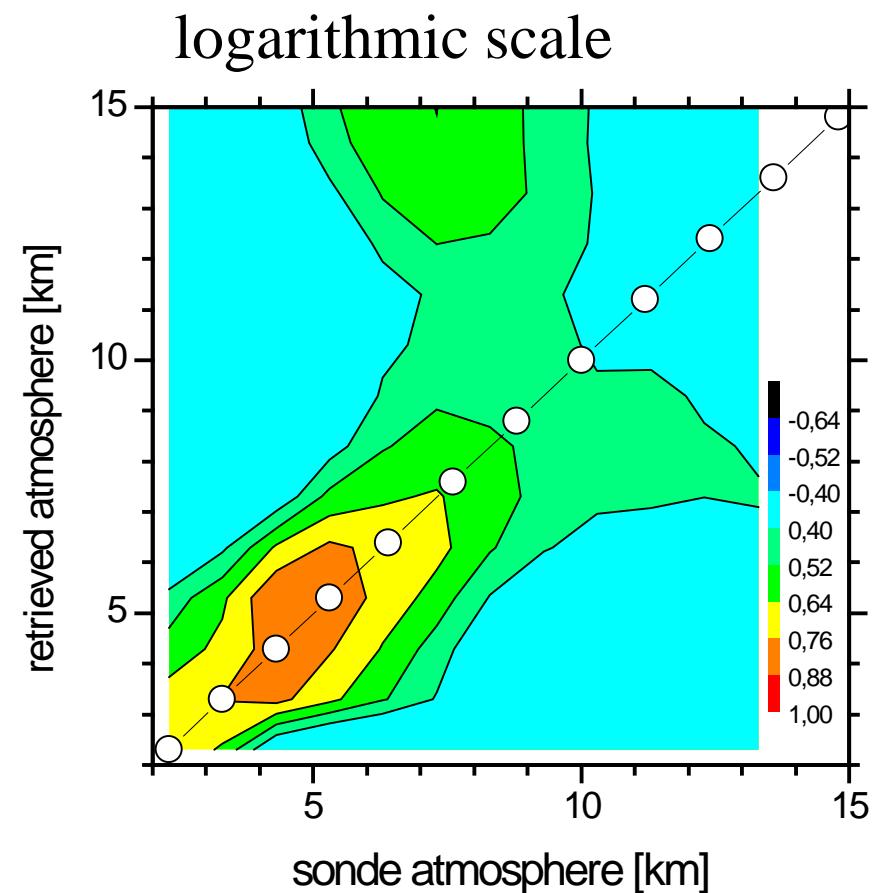
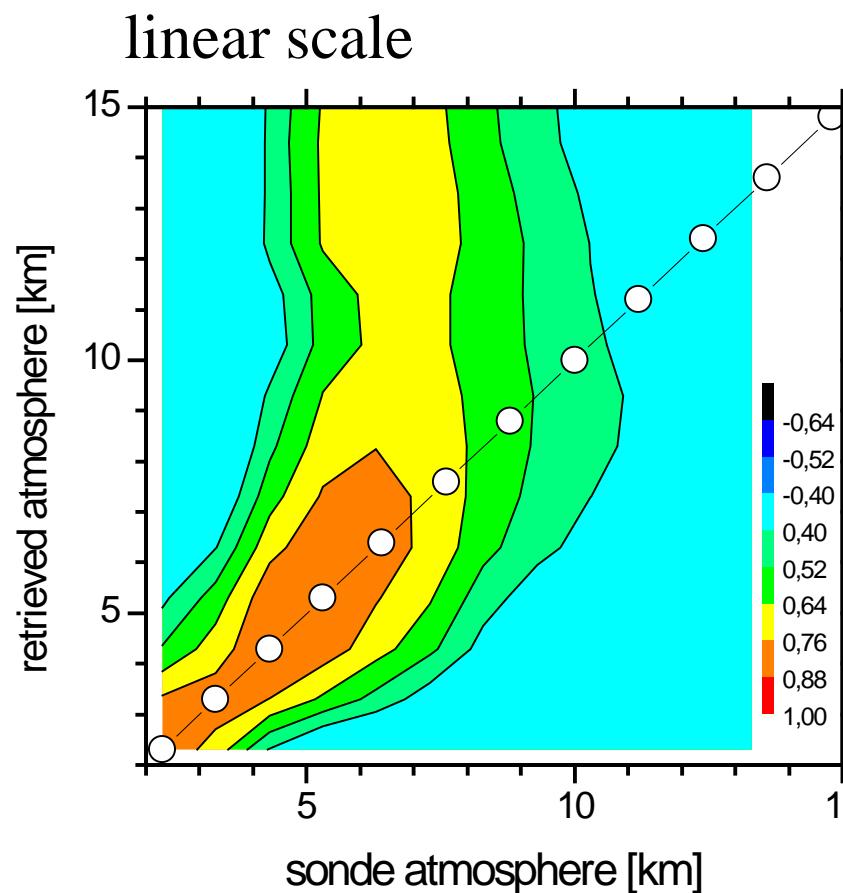
Inter-species constraint not only improves quality of  $\delta D$  profiles but also quality of H<sub>2</sub>O profile:

H<sub>2</sub>O retrieval benefits from additional information present in HDO lines

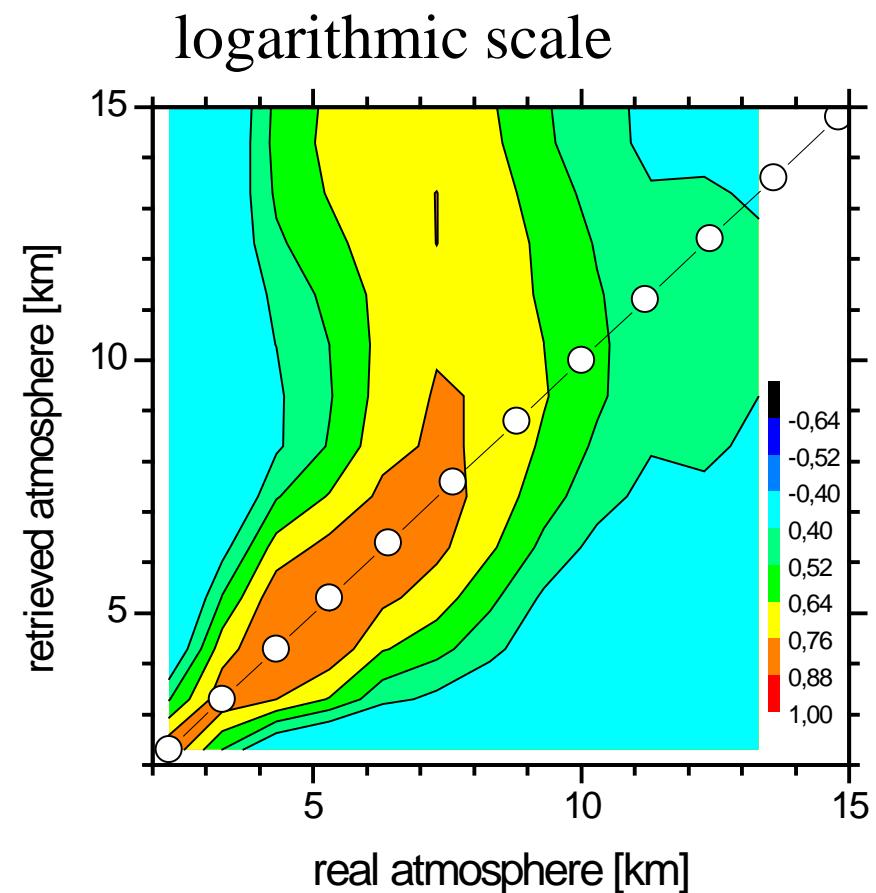
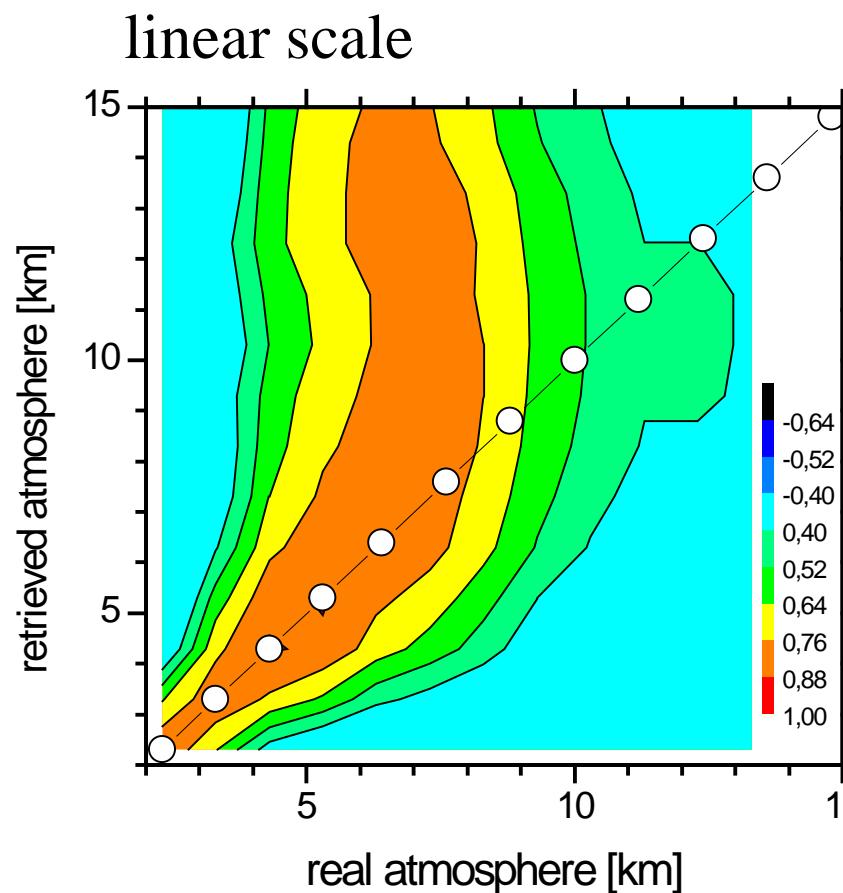
Detection of UT/LS H<sub>2</sub>O with the proposed lines ?

For a definitive conclusion we need a larger ensemble of compared profiles (the correlation shown here bases on only 7 profiles) !

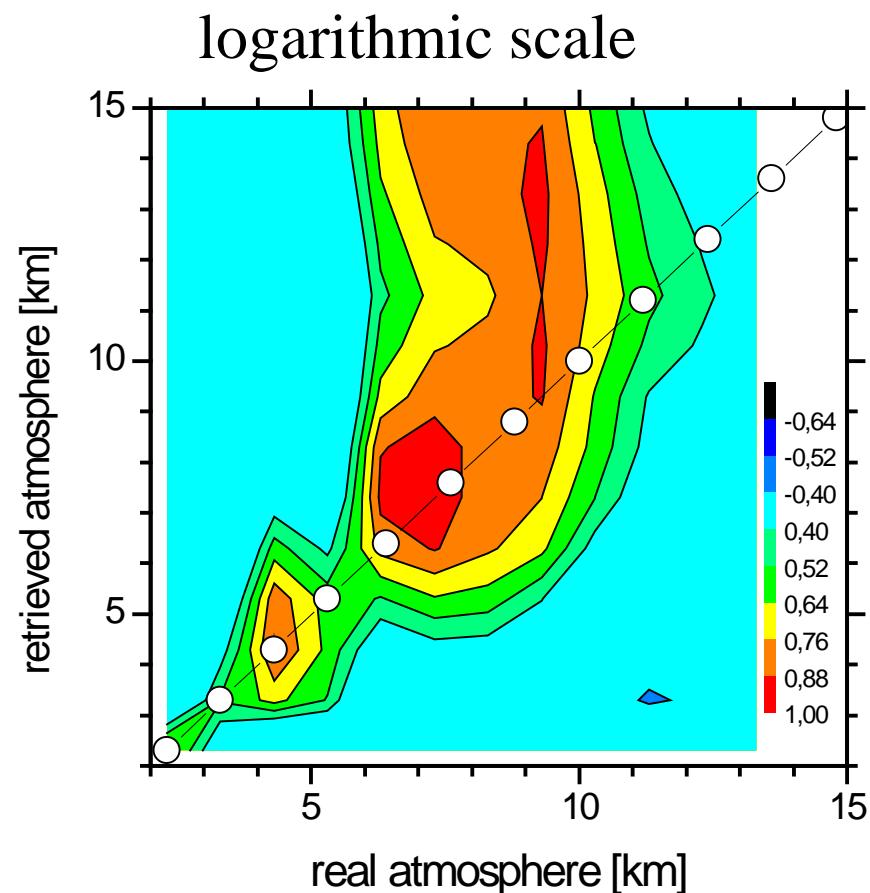
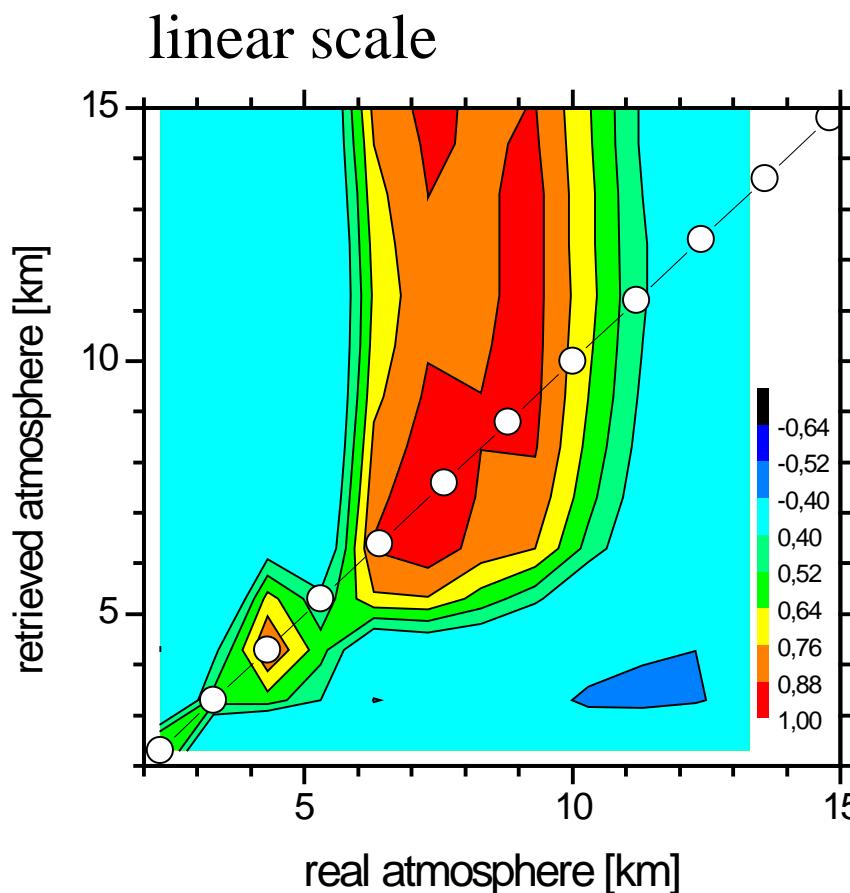
FTIR versus sonde profiles for all measurement days:



Corresponding theoretical sensitivity assessment (whole ensemble):

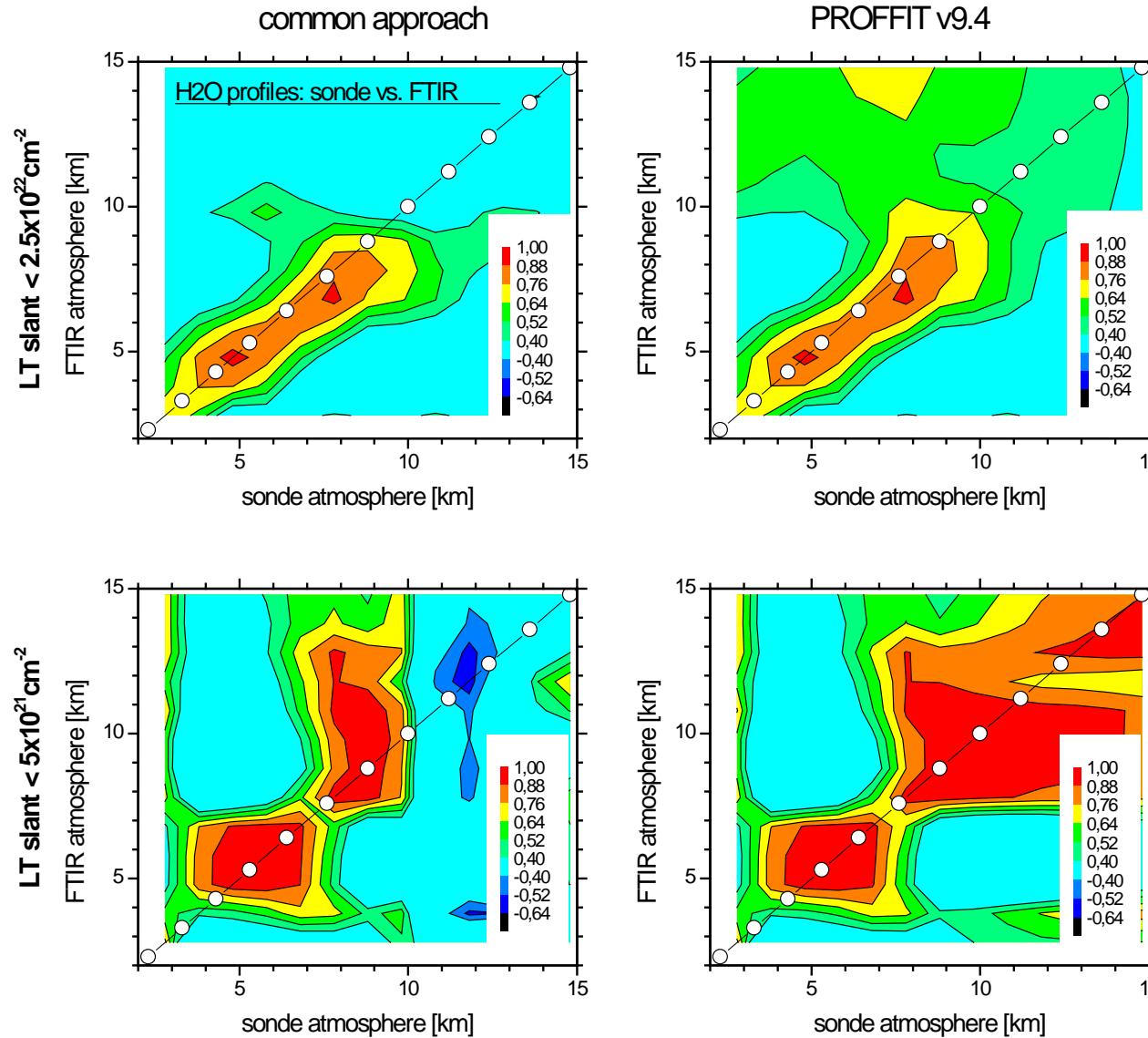


Corresponding theoretical sensitivity assessment (LT slant  $< 5 \times 10^{21} \text{cm}^{-2}$ ):



Slide from talk “Ground-based remote sensing of tropospheric HDO/H<sub>2</sub>O ratio profiles”

## Empirical validation of H<sub>2</sub>O profiles: ptu-sonde vs. FTIR:



Inter-species constraint not only improves quality of  $\delta D$  profiles but also quality of H<sub>2</sub>O profile:

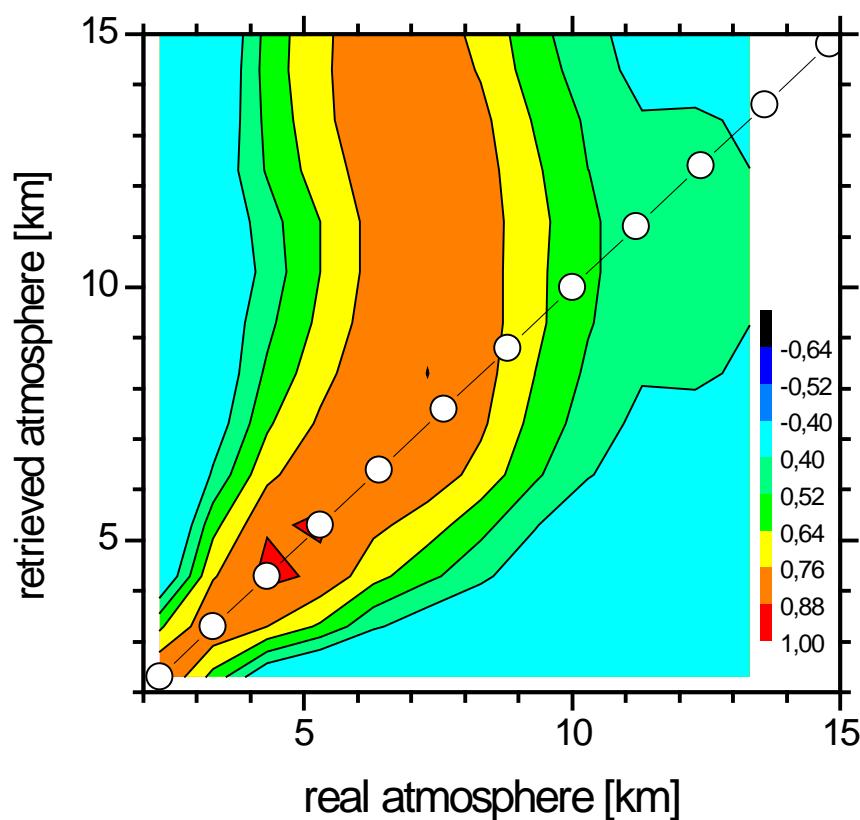
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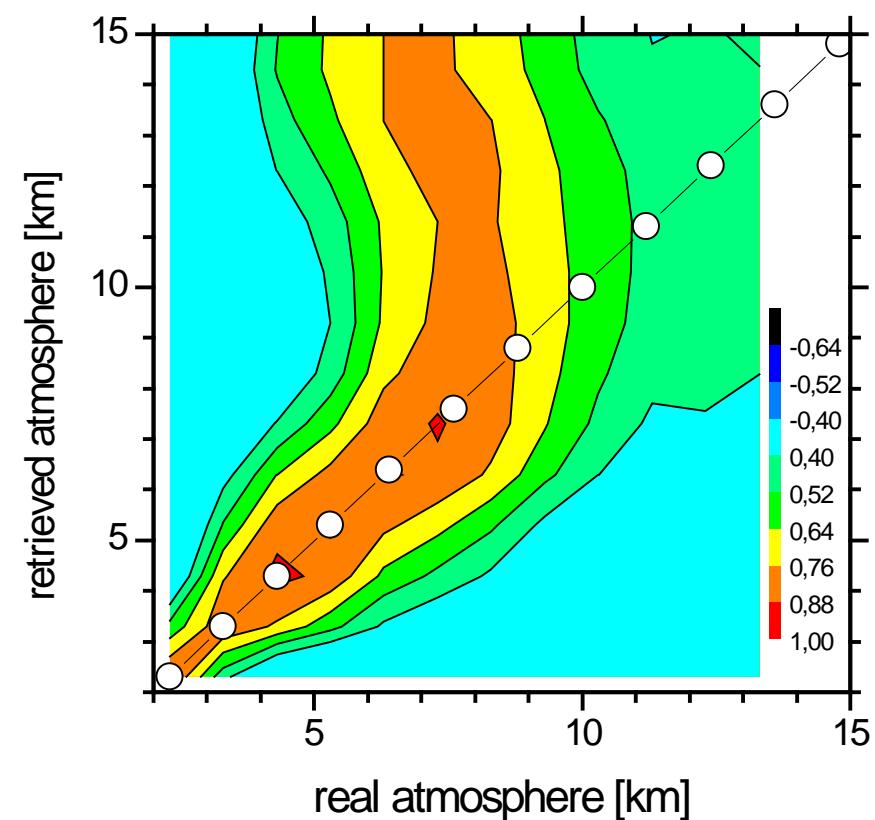
For a definitive conclusion we need a larger ensemble of compared profiles (the correlation shown here bases on only 7 profiles) !

Whole ensemble:

linear scale



logarithmic scale

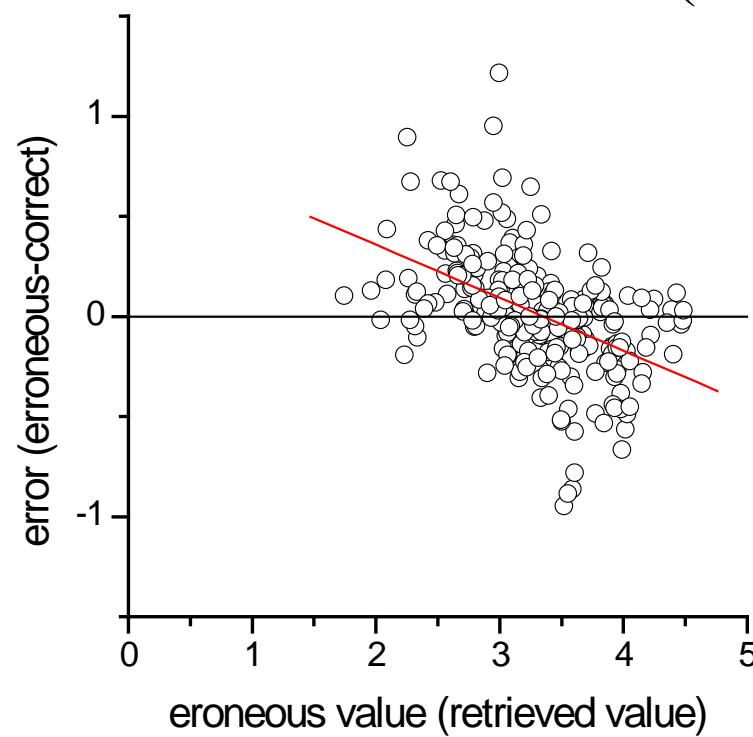
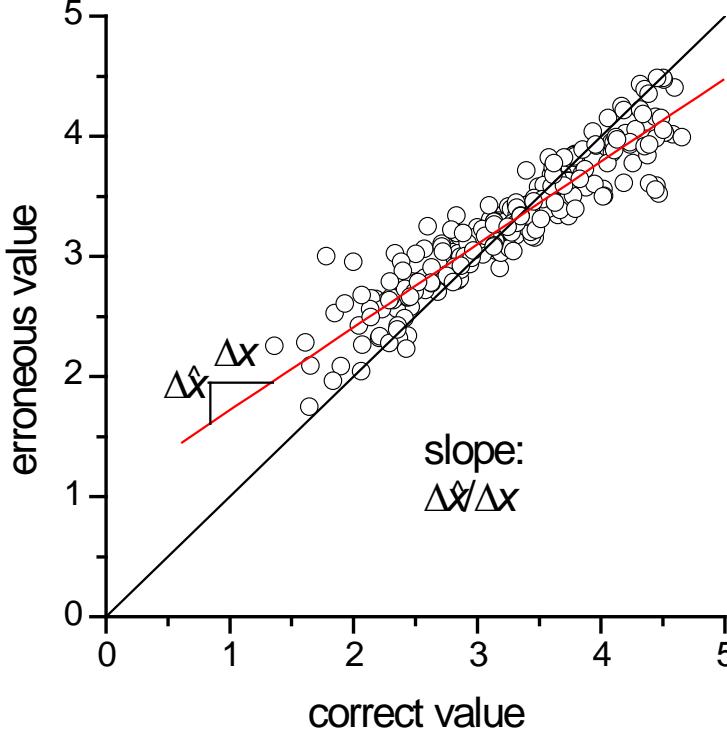


## Error estimation by means of linear least squares fit

Why? — there are two kind of systematic errors:

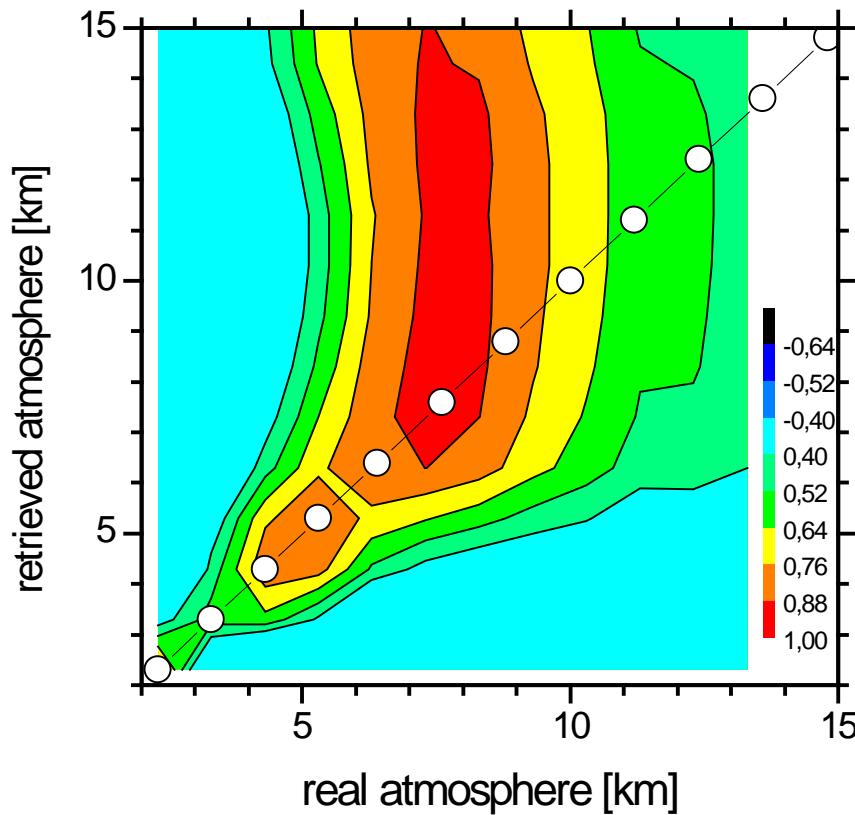
1. mean error (bias)

2. sensitivity error  
(slope $\neq$ 1)

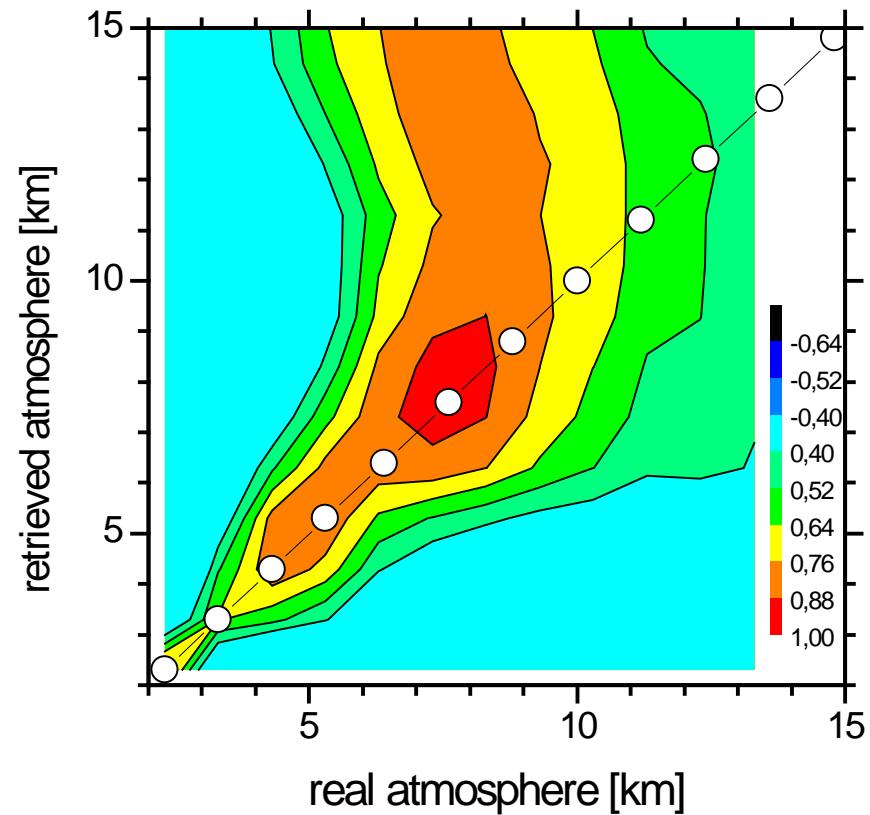


Slant column of lower troposphere (2.3-4.3km) below  $10 \times 10^{21} \text{cm}^{-2}$ :

linear scale

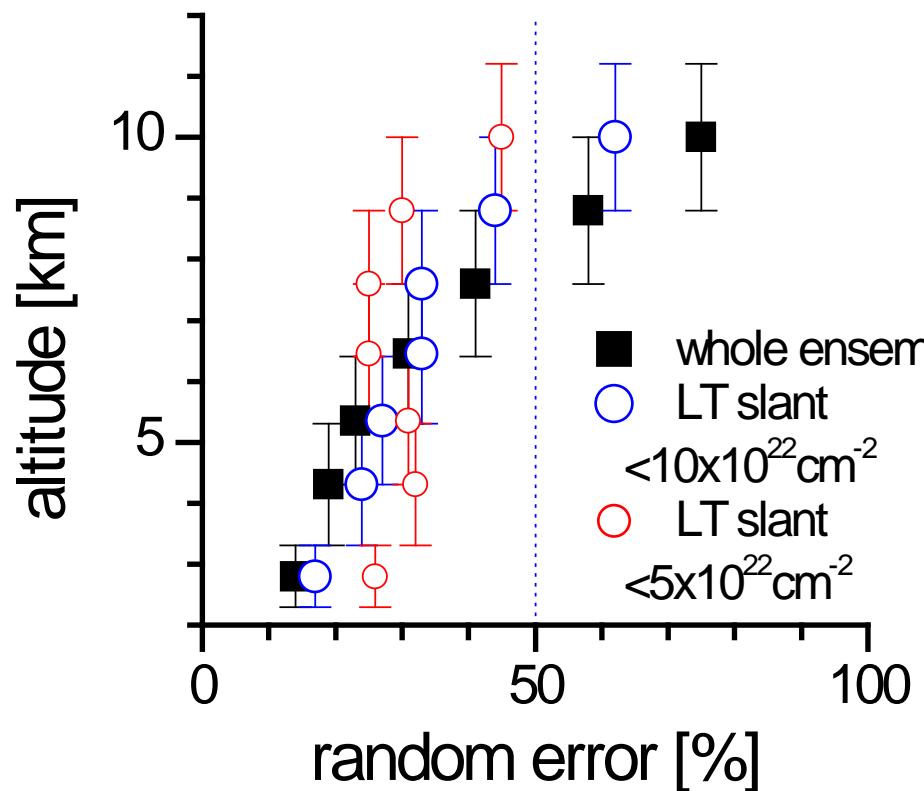


logarithmic scale

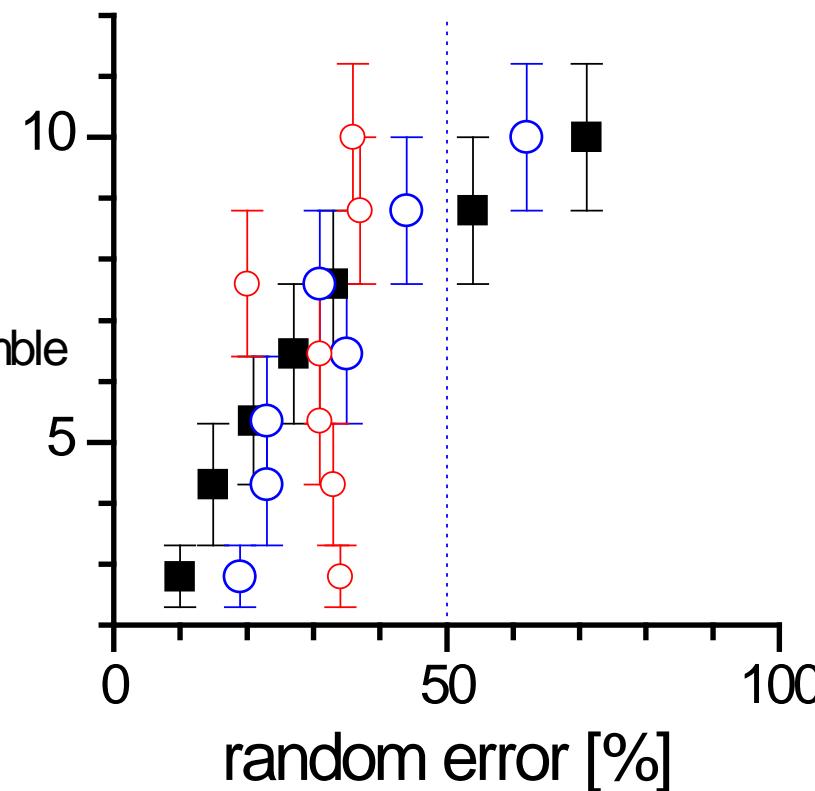


Summary of random error component of smoothing + measurement noise  
error:

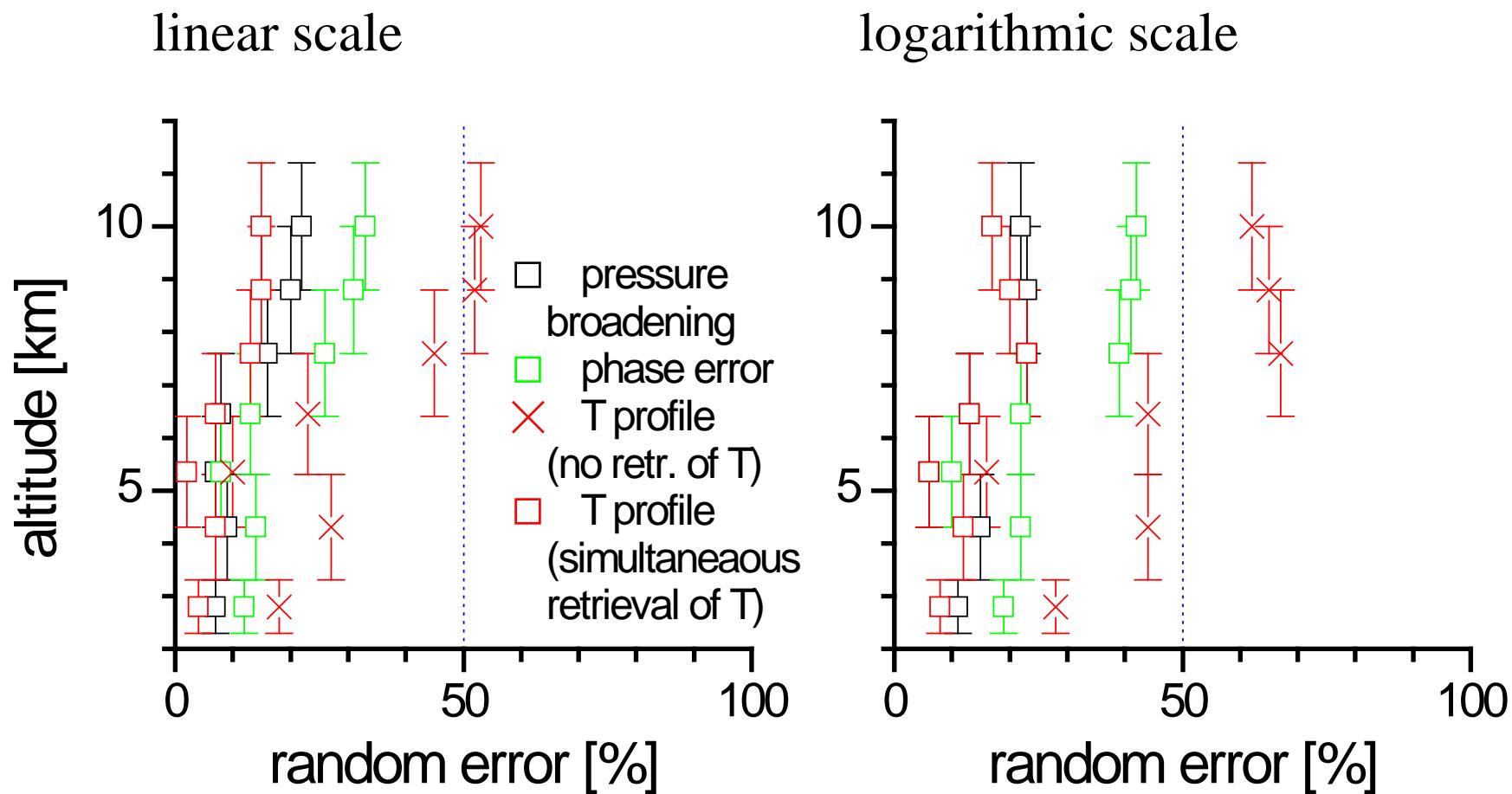
linear scale



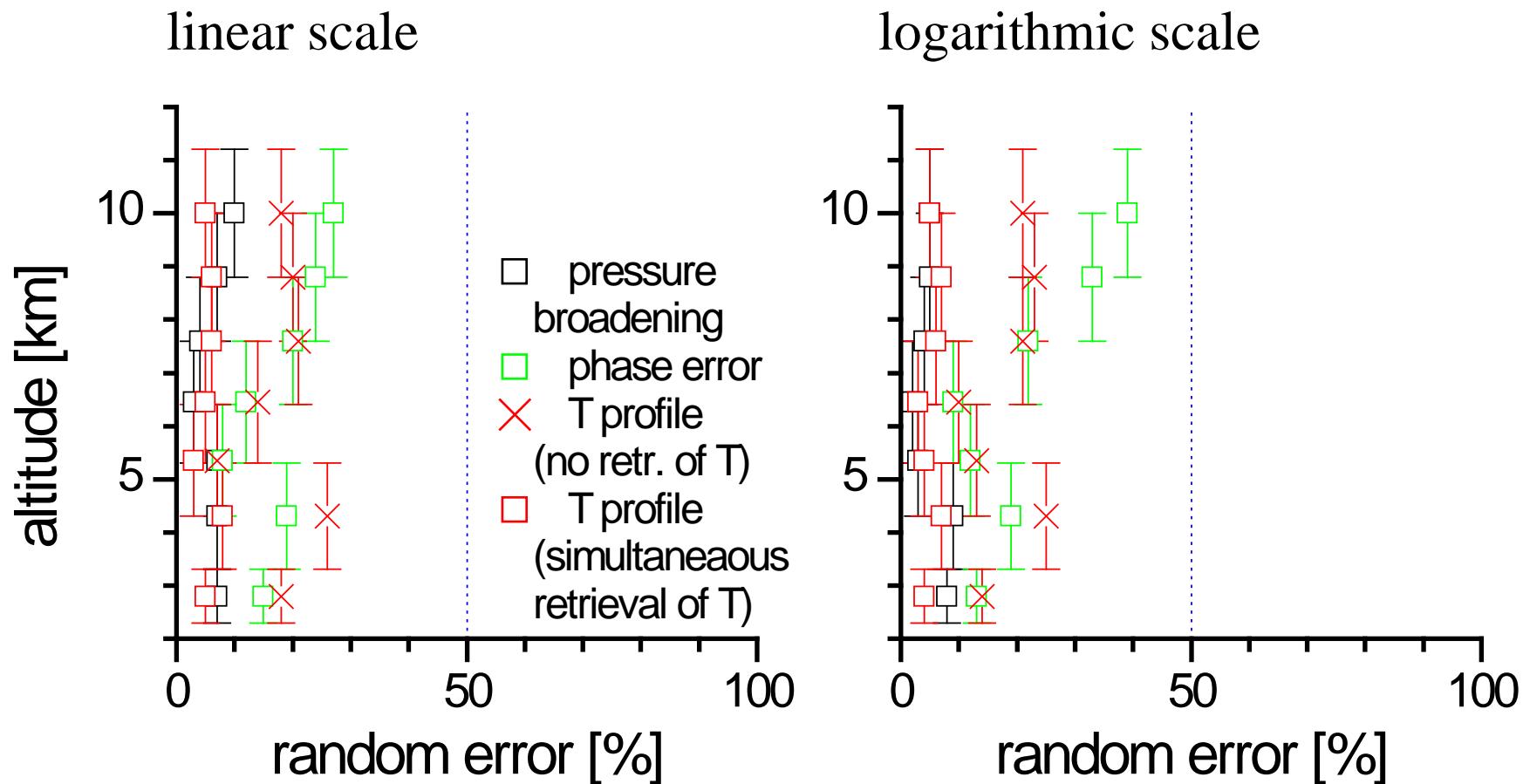
logarithmic scale



Summary of random error component parameter error (whole ensemble):

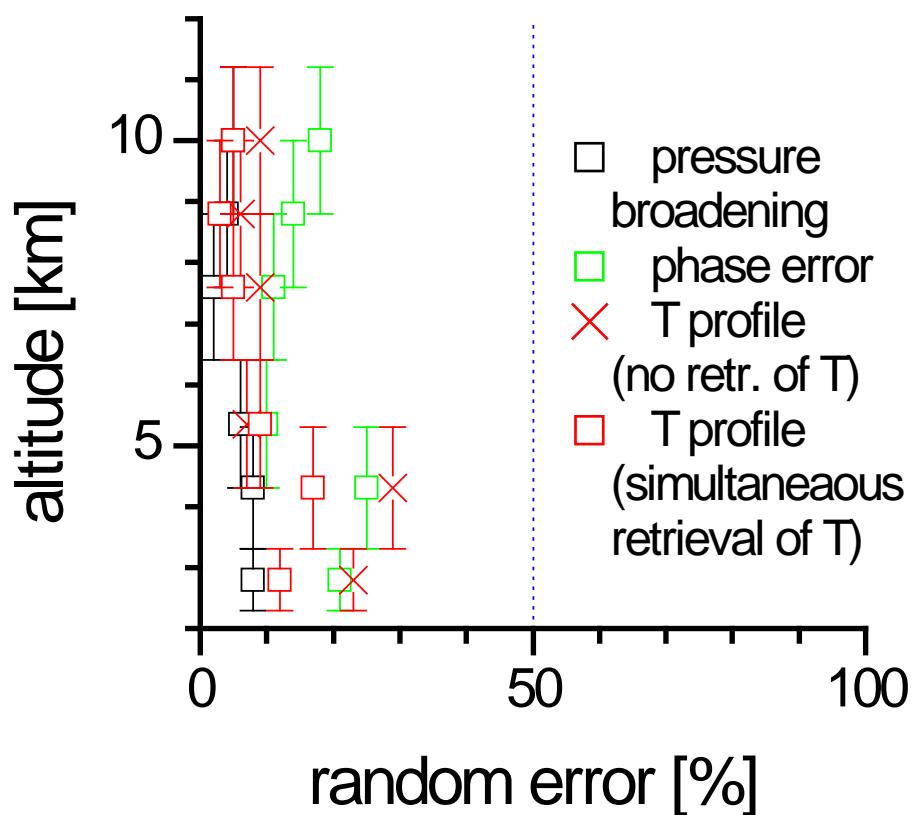


Summary of random error component parameter error (LT slant below  $10 \times 10^{21} \text{cm}^{-1}$ ):



Summary of random error component parameter error (LT slant below 5  
 $\times 10^{21} \text{ cm}^{-1}$

linear scale



logarithmic scale

